Surface Plasmon Polaritons for Magnetic Applications

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Surface Plasmon Polaritons (SPPs) are very useful for magnetic applications, especially for Heat Assisted Magnetic Recording (HAMR), magneto-optical sensing, and triggering magnons, because SPPs can be confined into a small spot beyond its optical interference limit. HAMR head is a good example for the application of SPPs\(^1\). Optical light is efficiently transferred into a SPP waveguide, and is effectively propagated to a Near-Field Transducer (NFT) at the end of the waveguide in HAMR head. A calculated result at a recording layer and a NFT tip at the end of SPP waveguide as an example is shown in Fig. 1. Magnetic sensing technique applying SPPs is also beneficial to sensitively detect magnetic condition\(^2\). Kretschman-Raether configuration at a critical incident angle as shown in Fig. 2 is very sensitive to reflective index. It can detect magnetization direction by its reflectivity of an incident light. For example, the reflectivity changes about 4 point at the incident angle \(\theta \sim 41\) degree as shown in Fig. 3. It could detect magnons distribution if we would apply NFT as a detecting sensor. As T. Satoh reported\(^3\), an optical light can trigger magnons, so SPPs must set off magnons if we control SPPs. We also found that the wavelength of SPPs can be controlled by a SPP waveguide structure as shown in Fig. 4\(^4\).

References

Acknowledgements
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Recent progress in fundamental studies on spin-photonics with magnets, semiconductors and insulators

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Digital information technology has great impact on our lives, which has strongly motivated scientists to look for faster and more energy-efficient ways to process streams of digital signals. This presentation reviews some works carried out recently in our group; namely, (i) devices for circular polarized light (CPL) technology and (ii) all-optical new functional devices.

Spin-LED as a monolithic CPL emitter (Fig. 1)
Compared with optics and photonics based on linearly polarized light, not so much research has been carried out for the development of technology based on CPL. We report bright electroluminescence of nearly pure circular polarization at room temperature with relatively high current density using lateral-type spin LEDs consisting of Fe stripe electrodes, 1-nm crystalline AlO$_x$ tunnel barriers, and laser-quality AlGaAs/GaAs double hetero-structures (DH) [1,2]. Electrical helicity switching up to 100 kHz has been demonstrated using dual spin injection electrodes formed on the DH [3,4].

From photo-excited precession of magnetization to all-optical new functional devices (Fig. 2)
We found through the study of photo-excited precession of magnetization using ultrashort (10^{-13} sec) weak laser pulses of 1 μJ/cm² or less, that spins in ultra-thin Co/Pd multi-layer films are very susceptible to light; namely, a material that could be a candidate for photo-sensitive magnets [5]. This finding has been followed by the demonstration of polarization modulation of light signals in an optical waveguide with the same class of magnets, GdFe thin films [6]. In this work, we have emphasized the feasibility of the multiplexed transmission of polarization-modulated signals, controlled ultimately by photo-excitation of a class of light-sensitive magnetic layers.

Reference
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Challenge to magnetization dynamics observation by Kerr microscope with real-time processing of differential-polarization images

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1. Introduction
In recent years, the functional spin-related devices that apply spin wave and the spin current have been developed. In most cases, these devices have been operated by detecting an electrical signal. However, the electrical signal might reflect not only the magnetic but also other properties, that it is important to verify other detection methods. The detection method by using magneto-optical effect is a useful detection method which has the advantages of non-contact and non-invasive. Additionally, Kerr effect microscope based on the photographic method is useful because it can visualize the two-dimensional spin propagation in a short time. We have been developed the Kerr effect microscope by photographic method 1-4. In general, conventional Kerr effect microscope which applies extinction method uses a saturation-image subtraction method 5 in order to emphasize the magnetic domain image. However, this method has the following problems; a sample with high saturation magnetic field cannot be observed; image deterioration caused by the position deviation of the sample which is affected by magnetic field and thermal expansion and efficiency of light is as low as a few percent. Accordingly, we report the development of Kerr effect microscope for observation of magnetization dynamics by differential-polarization imaging method, which can observe magnetization images in real time.

2. Principle of the differential-polarization imaging method
The schematic diagram of the differential polarization imaging method is shown in the Fig. 1. Light from the lamp illuminates the sample through a relay lens and an objective lens. The reflected light from the sample is imaged by the objective lens and the imaging lens. Images of two orthogonal polarizations are imaged separately by inserting the Glan-Thompson polarizing beam splitter between the imaging lens and the CCD camera. The analog video signals of the CCD camera 1 (CCD1) and the CCD camera 2 (CCD2) are amplified by the differential amplifier. Common background noises which are included in the both CCD camera images like the reflectivity change and so on are canceled by the differential amplifier. Kerr signal is increased by a differential amplifier because each signal is in the reverse phase. For this reason the output signal from the differential amplifier emphasizes the Kerr signal. These signals are captured into PC through the frame grabber with 8 bit brightness resolution. This method has the following advantages; magnetization image can be observed in real time, without application of saturation magnetic field; with no image deterioration according to positional deviation of the sample; the light utilization efficiency is high because of using all of the illumination light forms an image on the two CCD cameras.

3. Experiment
The optical system was arranged to measure the polar Kerr effect. The ample was a GdFeCo thin film with perpendicular magnetization. It was needed to perfectly match the images from each CCD camera to get a correct result. To accomplish this, the position, angle and focus of CCD1 were adjusted by using the pulse motor stage of the XYZθ axis. Electronic shutters of the CCD1 and CCD2 were set to 1/2000 seconds. An observation result of the maze magnetic domain of the GdFeCo thin film which is patterned to 40 × 100 μm is shown in Fig. 2. The images of CCD1 and CCD2 are shown in Fig. 2(a) and Fig. 2(b), respectively. The image of the difference between CCD1 and CCD2 is shown in Fig. 2(c). And the image which is obtained by the conventional extinction method is shown in Fig. 2(d). Domain structure is not observed in the image of Fig. 2(a) and (b) because the brightness change of the magnetic domain is less than the brightness resolution of the frame grabber. Maze magnetic domain structure has been observed in Fig. 2(c). In the differential polarization method, the obtained images contain hardware specific noise such as caused...
by a CCD camera and signal processing circuitry. To cancel the background noise which is caused by the hardware, the image which is recorded in the metal mirror is subtracted from the measured image. The image observed by the conventional extinction method is shown in Fig. 2(d) as comparison to the measurement result. Both Magnetic domain structure images of (c) and (d) are consistent. In conclusion, the present study has demonstrated that the magnetic domain image can be observed by the differential-polarization imaging method. Image of Fig.2 (d) has been acquired by setting the electronic shutter of the CCD camera to 1/30 seconds. The magnetic domain image was captured by the differential-polarization imaging method with light exposure of 1/67 less than the conventional extinction method. From these results, the Kerr microscope by differential-polarization imaging method is suitable for observation of magnetization dynamics using stroboscopic method. In the conference, the observation on longitudinal Kerr arrangement will be reported.

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Reference

Fig. 1 Schematic diagrams of the differential-polarization imaging method.

Fig. 2 Observation images and domain images for the GdFeCo thin film pattern (40 ×100 μm). Observation images of (a) CCD1 and (b) CCD2. Domain images of (c) differential-polarization imaging method and (d) conventional extinction method.
Artificial Magnetic Lattices and Their Optical and High Frequency Applications

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Artificial magnetic lattices (AMLs) introducing the artificial structure of the scale from a few 10 nm to several 100 nm show a novel magnetic functions attributed to their structures, so the studies utilizing these AMLs become an important engineering field. A magneto photonic microcavity (MPM) is a typical AML, in which transparent ferromagnetic garnet is sandwiched with two Bragg mirrors, and shows giant magneto-optical (MO) effect1). This presents a feasibility of new optical media controlling its optical properties by spin. On the other hand, the magnonic crystals, in which the light of MPC is replaced with the spin waves in ferromagnetic material, can control the precession of spin of the magnetic material and show the magnonic band gap2). In this symposium, these optical and high frequency applications using the artificial magnetic lattices are presented.

Holography is a key technology for three-dimensional (3D) displays, shape measurements, and high-capacity data storage. A holographic display is a realistic 3D display because it produces an exact copy of the wave front of scattered light from 3D objects3). Recently, we developed a 3D magneto-optic spatial light modulator (3D-MOSLM) that had a two-dimensional magnetic pixel array with sub-micrometer-scale pixels for a wide viewing holographic display. A thermomagnetic recording with an optical addressing method is used to form sub-micrometer-scale magnetic pixel arrays without a driving line, and 3D image is reconstructed using the MO effect. The first 3D-MOSLM used an amorphous TbFe (a-TbFe) film as magnetic film4), but the brightness of reconstructed images was very low. To achieve bright 3D images, the magnetic film should have high transmittance and a large Faraday rotation angle, so we developed a 3D-MOSLM with MPM structure using the Bi substituted rare earth iron garnet (Bi:RIG) as a recording magnetic layer. As a result, as shown in Fig. 1(b)-(d), we could achieve the reconstruction 3D image as bright as 100 cd/m² by using the designed 3D-MOSLM having a MPM structure with high diffraction efficiency5). Another application of holography is the hologram memory that is a promising candidate for next data-storage technology with high recording densities of greater than 1 TB/disk. We have employed a collinear holographic system that can write and read data using a single optical axis with a spatial light modulator6). Similar to 3D-MOSLM, we have also selected the Bi:RIG film as a recording medium, and succeeded to record and reconstruct data on the Bi:RIG film using the collinear holographic system as shown in Fig. 2(a)7). However, the reconstructed image was dark and unclear due to the low diffraction efficiency of the garnet medium. To improve the diffraction efficiency, we again designed MPM structures for the recording medium. Figure 2(b) and (c) show the reconstructed images from the usual single layer garnet film and the MPM medium8). The image reconstructed from the MPM medium had approximately twice the brightness of that reconstructed from the single layer film. These mean that the MPM structure is very attractive recording media.

In addition to these optical applications, we also apply the AML structure to control the magnetostatic waves (spin waves), which is supported by the magnetostatic coupling of spins in a few GHz frequency region. An analogy of photonic crystal, when the propagation medium such as YIG have some periodicity, a magnonic band gap (MBG) can be observed for the spin waves. This MBG can be designed within an excitation frequency band by selecting the appropriate periodicity of the metal strips. We demonstrated experimentally the existence of the MBG using the sample with the one-dimensional periodic structure of Cu strip as shown in Fig. 3. As shown in Fig. 3(b), a clear and deep band gap was observed at approximately 3.00 GHz, and the frequency of the band gap is very sensitive to the magnetic field applied to the crystal9). This high-<i>Q</i> MBG would be used for magnetic sensor. Similar to MPM, the localized mode of spin wave was also observed as shown in Fig. 3(d) by introducing a defect layer in periodic structure9). These results indicate that we can manage the spin wave propagation in the same manner as the light in photonic crystals using AML structure although we have to consider the effect of shape magnetic anisotropy of the spin-wave waveguide.

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Fig. 1 (a) A model of 3D image for generating the hologram. The wireframe cube was constructed by point light sources. (b)–(d) Reconstructed images from MPC and (e)–(g) those from α-TbFe for comparison. The images of (b) and (e) were from left view point of 11°, (c) and (f) were from center, and (d) and (g) were from right view point of 11°.

Fig. 2. Experimental setup and reconstructed two-dimensional data patterns. (a) Schematic illustration of the experimental setup for writing and reconstructing magnetic holograms. Reconstructed signal patterns from (b) the single layer Bi:RIG film and (c) the two-pair MPC medium. The MPC medium provided a clear and bright image because the diffraction efficiency of MPC medium was as double as that of the single layer film.

Fig. 3. (a) Schematic illustration and photograph of the 1D magnonic crystal composed of a YIG single crystal film and a periodical metal strips. (b) Frequency shift in the magnonic band gap corresponding to the change in the bias field from 200 Oe to 204.5 Oe with an interval of 1.5 Oe. (c) Schematic illustration of a magnonic crystal in the shape of a microcavity. (d) Transmission spectrum showing a localized state of spin wave at 3.395 GHz under the applied magnetic field of 400 Oe.

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Ultrafast photo manipulation of magnetization
and non-local spin dynamics

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For further progress in applications on magnetic magnonic and spintronic technology, ultrafast control of magnetization (ordered spin system) is an issue of crucial importance. Controlling magnetism by light is one of the promising approaches as appealing scenario. For photo manipulation of magnetization, femtosecond laser pulses that are among the shortest stimuli in contemporary technologies could serve as an alternative stimulus to manipulate spin order and trigger magnetization reversal.

An ultrashort laser pulse allows excitation of magnetic systems at time scales much shorter than fundamental quantities such as spin precession or spin-lattice relaxation times. Deterministic magnetization reversal was demonstrated\(^1\)\(^2\) in ferrimagnetic GdFeCo driven by single shot irradiation of laser pulse without the presence of a magnetic field. This All Optical Switching (AOS) phenomena originated from transient non-equilibrium state and sub-lattice nature is fundamentally different from conventional magnetic field driven switching mechanism. Furthermore, from the compositional dependency of all-optical light helicity-dependent magnetic switching (AO-HDS) in ferrimagnetic GdFeCo alloy, it is found that AO-HDS is associated with the collinear sub-lattice magnetization and an explanation of the AO-HDS based on magnetic circular dichroism exactly matches the above features of experiments\(^3\).

Recently, it is revealed that further extraordinary spin dynamics in ultrashort time scale such as bellow ps region by ultrafast diffraction experiments with an X-ray probing\(^4\). In particular, we observed Gd spin reversal in Gd-rich nano-regions within the first picosecond driven by the non-local transfer of angular momentum. These results suggest that a magnetic microstructure can be engineered to control transient laser-excited spins, potentially allowing faster spin reversal. Furthermore, AOS depends on the non-adiabatic energy dissipation of electron system in the GdFeCo layer from the incident surface in the depth direction during a few picoseconds\(^5\). It will be also shown that employing plasmonic gold nano-antennas placed above TbFeCo magnetic layer it should be possible to confine photo-magnetic excitation in a spot well below diffraction limit as the order of 50 nm\(^6\). Ultrashort non-local phenomena in magnetic material will be discussed.

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Reference
All-optical investigation of coherent magnon propagation in metallic films

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Dipolar spin-wave frequency is typically in GHz microwave range and its lifetime is quite long in some materials, such as yttrium iron garnet (YIG), thus spin-wave have been widely studied to apply passive and active microwave devices in early days. Most of them could not be commercialized since those were not beyond semiconductor devices. Nowadays, spin-wave or its quantum, magnon, is studied with renewed interest as a basis for Magnonics, spin-based information processing technology without electric charge to reduce power consumption.\(^1\) The Magnonics research is still fundamental, where various basic building blocks have been discussed from the various aspects.\(^2\)\(^,\)\(^3\) The light-induced coherent magnon may be one of such building blocks, which has been studied during the past few years,\(^2,\)\(^3\) because it is applicable to a light coupling for magnon circuit interconnection.\(^2\) It is also interesting to seek light-induced coherent magnon in metallic films, because magnon dispersion in metallic film hetero-structure can be tuned by the interfacial anti-symmetric exchange interaction and also the externally applied electric field.\(^4\)\(^,\)\(^5\) However, there have been few reports on the light-induced coherent magnon in metallic films.\(^5,\)\(^6\)

Here we present our recent results on the propagating magnon excited in films of magnetic metals by the micro-focused fs pulse laser with the spot diameter of \(\mu\)m scale. The magnon-propagation induced by the laser pulse was detected via the magneto-optical Kerr effect for another weak laser pulse with varying position and delay-time using all-optical scanning pump-probe technique (Fig. 1). The pulse laser-induced coherent magnons propagation was clearly observed and its propagation were highly anisotropic with respect to the direction of magnetization (Fig. 2), being consistent with the anisotropic dispersion of magneto-static surface or backward volume wave. Excitation mechanism of magnon is discussed in terms of ultrafast change of magnetization induced by the pulse laser.\(^7\) This work was partially supported by KAKENHI No. 16H03846, Nano-spin conversion science No. 26103004, and the center of Spintronics Research Network.

Reference
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Fig. 1 Schematic illustration of the all-optical spatio-temporal pump-probe measurements for magnetic film under microscope.

Fig. 2 Spatio-temporal mapping of the experimental data of the pump-pulse-induced change of Kerr rotation angle. The scanning direction of probe beam is (a) x- and (b) y-axis.
Accumulative magnetic switching of FePt granular media by circularly polarized light

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Deterministic control of magnetization by light, often referred to as all-optical switching (AOS), is an attractive recording method because magnetization control becomes possible without the need of an external magnetic field¹-⁵. The first demonstration of AOS was in ferrimagnetic GdFeCo film where the Gd and FeCo spin sub-lattices are antiferromagnetically exchange coupled. Since the mechanism determined for GdFeCo films required antiparallel exchange of two sublattice systems, it was believed that AOS occurs only in ferrimagnetic materials including synthetic structures¹-⁴. However, recently Lambert et al. reported that the optical control of the magnetization occurs in ferromagnets including Co-based multilayer thin films and FePtAg-C granular thin film materials⁵. Therefore the potential mechanisms for AOS in ferromagnetic materials must be reexamined. Here, we report the observation of accumulative magnetic switching from multiple circularly polarized light pulses on FePt-C HAMR media.

The FePt-30vol%C (hereafter, FePt-C) granular film was deposited by co-sputtering of FePt and C targets on a MgO(001) single crystal substrate by DC magnetron sputtering at 600°C. 10-nm-thick C was deposited as a capping layer at RT. 15-µm-width Hall crosses were used for the measurement of the magnetization change by the light exposure and the applied magnetic fields.

Figure 1(a) shows the magneto-optical image of an initially demagnetized FePt-C granular film after scanning it with both right and left circularly polarized (RCP and LCP) light pulses. The optical pulses induce a net magnetization in the FePt-C and the sign of the magnetization is determined by the helicity of the light. To quantify the optically-induced magnetization changes, we exposed the laser over the Hall cross region. The initial state is remanence after applying saturating magnetic fields of -7 T (Fig. 1c)) and 7 T (Fig. 1d)). Figure 1(c) shows the normalized Hall resistance change after the exposure to RCP, linearly polarized and LCP. For RCP light, the normalized magnetization gradually decreases to zero, then reverses and saturates at about -0.5. This indicates that ~3/4 of the FePt grains switch to the opposite direction. On the other hand, the exposure to LCP light decreases the magnetization to about half of the initial value, corresponding to the switching of ~1/4 of the FePt grains. For exposure to linearly polarized light, the normalized magnetization gradually approaches zero. In the case of the opposite initial state (negative saturation) shown in Fig. 1d), RCP, LCP and linearly polarized light exposures result in the same final normalized magnetization of -0.5, 0.5 and zero, respectively. Thus, the magnetization state after exposure to polarized light only depends on the helicity of the light. Fitting Fig. 1(c) and (d) to a simple accumulative model, the switching probability by a single pulse is very small, less than 1%. However, accumulating the small switching probabilities results in a continuous change in the magnetization until the final equilibrium state⁶.


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Fig. 1 Magnetization change observed from a FePt-C granular film by exposure to circular polarized light. (a) Magnetic image after exposure to RAP and LCP. (b) AHE curve for the FePt-C granular film. (c,d) Normalized Hall resistance after applying circular and linear polarized light.
Magnetization control using ultrashort optical pulses has been extensively studied in recent years. One of the nonthermal control of magnetization is based on the inverse Faraday effect, where circularly polarized pulses generate the effective magnetic field along the propagation vector in a transparent material, leading to spin wave generation\(^1,2\)). Spin wave reflection at the sample edge or transmission through an air gap has been reported in finite-size samples\(^3,4\)). In the present study, we report on time- and phase-resolved imaging of photo-induced spin wave’s transmission through an air gap using pump-probe technique with a CCD camera.

In the experiment, a bismuth-doped rare earth iron garnet crystal with a thickness of 110 \(\mu \text{m}\) was used as a sample. Circularly polarized pump pulses with a time duration of 150 fs were employed to excite the sample via the inverse Faraday effect. Faraday rotation of time-delayed probe pulses was measured. Figure 1 shows the transmission of spin wave excited in the left hand sample through an air gap to the right hand sample, where the gap width was 40 \(\mu \text{m}\) and the time delay was 1000 ps. The center wavelength of the spin waves was observed to be 100-200 \(\mu \text{m}\) meaning that the spin waves were dipolar-dominated magneto-static waves. The relation between transmission, phase and the gap width was analyzed. The experimental results were compared with simulation results.

Reference

Acknowledgements
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Spin transfer torque (STT) switching is considered as a promising technology to realize Gbit class magnetic random access memories (MRAMs). However, there still remains a challenge to develop high-density MRAMs with densities of several Gbit and beyond, since it has a conflicting requirement, i.e., a reduction of critical current density $J_c$ to switch the memory cell while keeping a sufficient thermal stability of the cell. One of the solutions for this challenge is so-called thermally assisted MRAM in which the memory layer is heated during the writing\textsuperscript{1).} We have studied amorphous TbFe\textsuperscript{2), 3)} and GdFeCo\textsuperscript{4), 5)} as a memory layer of the thermally assisted MRAM cell. In this paper, we discuss the STT switching of GdFeCo single layers and GdFeCo / TbFe exchange coupled bilayers. Moreover, Gilbert damping constant $\alpha$ of GdFeCo / TbFe bilayers is discussed to compare the product of Gilbert damping and perpendicular anisotropy with the switching current density $J_c$.

GdFeCo ($10 - x$ nm) / TbFe ($x$ nm) exchange coupled bilayers were deposited on thermally oxidized Si substrates by RF magnetron sputtering, where the TbFe thickness $x$ was varied from 0 to 5 nm. Time resolved magneto-optical Kerr effect (TRMOKE) measurements were carried out to estimate Gilbert damping $\alpha$ and anisotropy field $H_k$ of the bilayer.

Figure 1 (a) shows TbFe thickness dependence of Gilbert damping constant $\alpha$ of the bilayer. The damping constant $\alpha$ of the GdFeCo / TbFe was relatively low 0.051 for $x = 0$, and it significantly increased to 0.23 for $x = 1$. TbFe thickness dependence of the anisotropy field $H_k$ estimated from the TRMOKE measurements was shown as closed circles in Fig. 1 (b). The $H_k$ gradually increased with increasing TbFe. The $H_k$ estimated from TRMOKE agreed well with the $H_k$ estimated from hysteresis loops which is shown as open circles in Fig. 1 (b). We compares the product $\alpha \times M_s H_k$ of the as-deposited GdFeCo / TbFe bilayers with the $J_c$ of CIMS as shown in Fig. 1 (c), since the $J_c$ is known to be proportional to the product, $\alpha \times M_s H_k$, in a single memory layer. The $J_c$ of the GdFeCo (9 nm) / TbFe (1 nm) was confirmed to increase by 1.6 times compared to that of the GdFeCo (10 nm), while the product $\alpha \times M_s H_k$ was confirmed to increase by a factor of 10. This suggests that an empirical relation, $J_c \propto \alpha \times M_s H_k$, does not hold in the exchange coupled bilayer system.

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