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Journal

### Magnetic Recording

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# JOURNAL OF THE MAGNETICS SOCIETY OF JAPAN

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Physicist

**Peter Grünberg**

## 未来をどこまで想像できるか。

進みつづける時間の先に、何を見るか。

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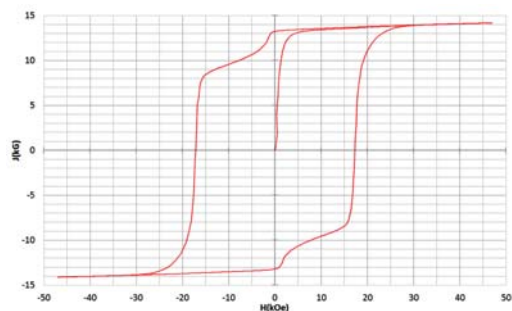
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0.5mm cube磁石のBr, HcJ高精度測定が可能と  
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\*2014年7月 東英工業調べ

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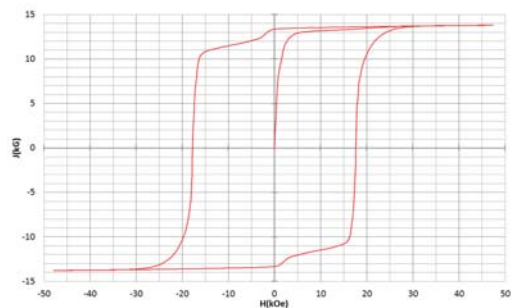
高温超電導VSMによるNdFeB(sint.) 0.5 mm cube BHカーブ



磁化測定レンジ: 0.2 emu

Br = 13.2 kG HcJ = 17.2 kOe

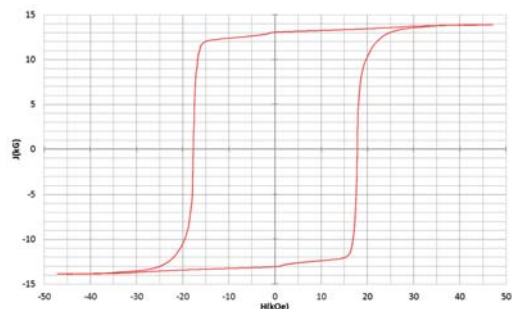
高温超電導VSMによるNdFeB(sint.) 1 mm cube BHカーブ



磁化測定レンジ: 2 emu

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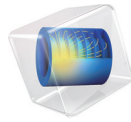
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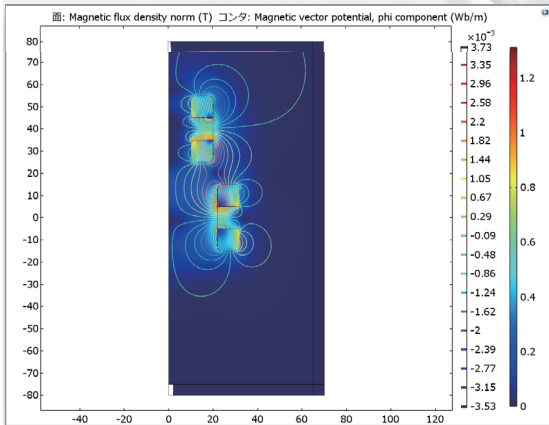
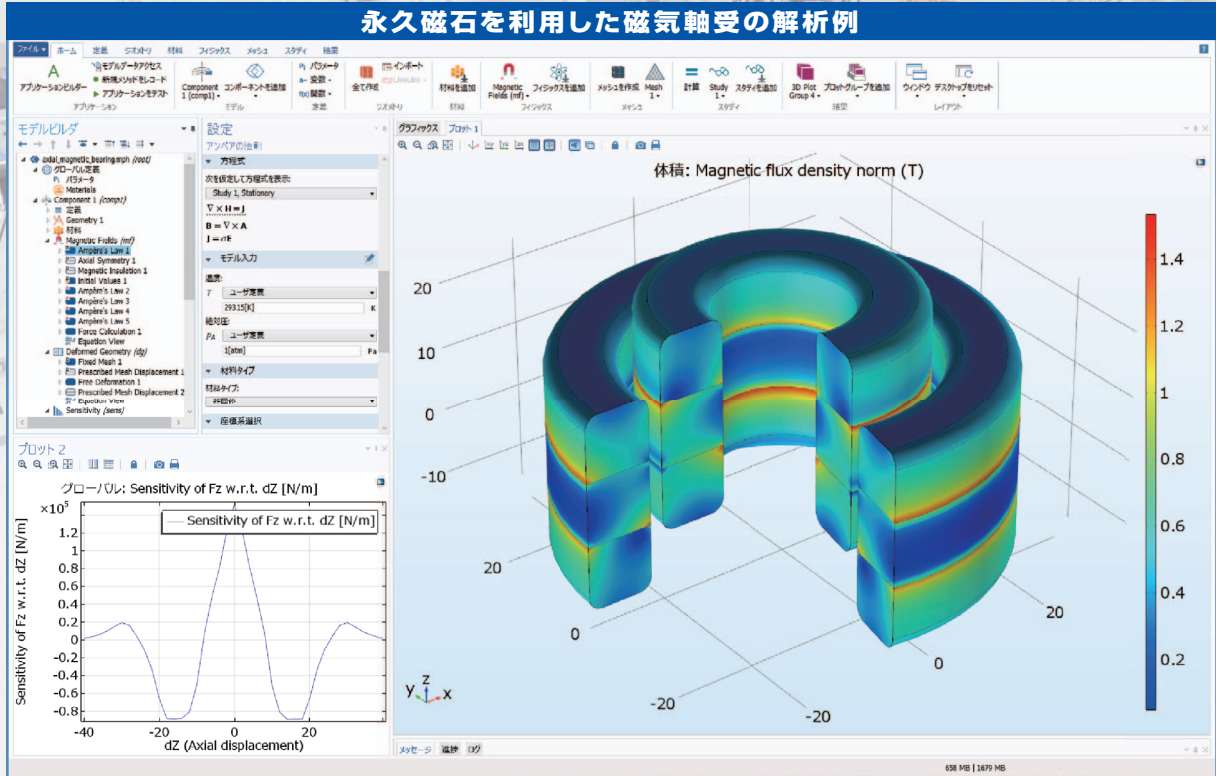


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- ホール効果を利用したセンサ
- インシュレータ、コンデンサ、誘電体
- モータ、ジェネレータ、および他の電気機械
- 非線形材料
- 寄生容量とインダクタンス
- 永久磁石と電磁石
- 多孔質材料
- 抵抗および誘導加熱
- センサ
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- 変圧器とインダクタ

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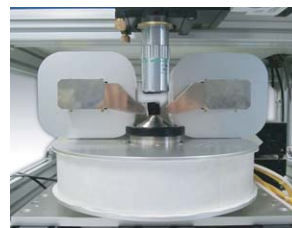
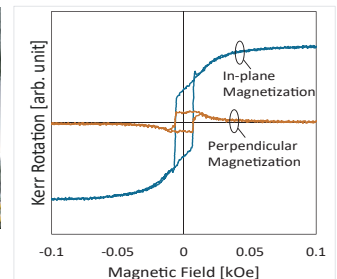
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面内 / 垂直磁場発生可能な  
3 極電磁石

測定例

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# A New Model Calculation Using Probability for Heat-Assisted Magnetic Recording

T. Kobayashi, F. Inukai, K. Enomoto, and Y. Fujiwara

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We propose a new model calculation using the reversal probability of grain magnetization for heat-assisted magnetic recording (HAMR). Our new model calculation can obtain the bit error rate as a function of the writing field  $H_w$  for a given anisotropy constant ratio  $K_u / K_{\text{bulk}}$ , which is a new parameter that we introduced. The physical implication of the recording time window proposed in the micromagnetic calculation is discussed using the new model calculation. Although the recording time window is a good guideline for write-error and erasure-after-write (EAW), EAW cannot be determined solely by the recording time window. The influence of EAW is accurately examined. The allowable range of  $H_w$  and  $K_u / K_{\text{bulk}}$  is also provided for various Curie temperatures  $T_c$ .  $T_c$  and the heat-transfer thermal gradient are important parameters for reducing  $K_u / K_{\text{bulk}}$ .

**Key words:** heat-assisted magnetic recording, model calculation, anisotropy constant ratio, recording time window, Curie temperature, thermal gradient

## 1. Introduction

Various methods have been proposed with the aim of increasing the areal density of magnetic recording beyond the trilemma limit<sup>1)</sup> for granular media. The methods include shingled magnetic recording (SMR), the use of media with a relatively large grain size or bit patterned media (BPM), heat-assisted magnetic recording (HAMR), and microwave-assisted magnetic recording.

It has been reported that the medium thermal stability factor  $K_u V / kT$  must exceed 60 to ensure that the grain magnetization direction remains stable during 10 years of archiving, where  $K_u$ ,  $V$ ,  $k$ , and  $T$  are the grain anisotropy constant, the grain volume, the Boltzmann constant, and temperature, respectively. In our previous papers<sup>2, 3)</sup>, we evaluated the statistical thermal stability factor  $\text{TSF}_{10}$  corresponding to a value of 60, that is,  $K_u V / kT > \text{TSF}_{10}$ , and we showed that the minimum  $K_u$  value for the stability is reduced by decreasing the grain number per bit (increasing the grain size) since  $V$  increases despite the fact that  $\text{TSF}_{10}$  increases. Furthermore, we also showed that the standard deviation of the dot size for BPM must be restricted to a small value.

We have already reported a HAMR model calculation<sup>4)</sup> using  $\text{TSF}_{10}$  in order to shorten the calculation time and grasp the physical implications. In that paper, we introduced the anisotropy constant ratio  $K_u / K_{\text{bulk}}$  as a design guideline.  $K_u / K_{\text{bulk}}$  is the intrinsic ratio of medium  $K_u$  to bulk  $K_u$ . We must design a medium with a smaller  $K_u / K_{\text{bulk}}$  if we are to achieve good media productivity. We have subsequently improved our model calculation by introducing a statistical thermal stability factor during writing, and we revealed the dependence of the minimum  $K_u / K_{\text{bulk}}$  value on the change of one parameter among many design parameters<sup>5)</sup>. As a result, we found that

increasing the writing temperature  $T_w$  is only effective for reducing  $K_u / K_{\text{bulk}}$ . We also provided examination results for a combination of more than two parameters<sup>6)</sup>. In conclusion, the combinations that can reduce  $K_u / K_{\text{bulk}}$  always have SMR as one parameter. However, the use of SMR sometimes degrades the read/write performance of the hard drive. Although a lower  $T_w$  is better in terms of the heat resistance of the writing head and/or the surface lubricant, increasing  $T_w$  appears to be the only way of reducing  $K_u / K_{\text{bulk}}$  for HAMR media. Increasing  $T_w$  has many advantages in addition to reducing  $K_u / K_{\text{bulk}}$ <sup>7)</sup>. We have recently improved our model calculation<sup>8)</sup> by introducing the concept of the recording time window<sup>9)</sup> proposed in a micromagnetic simulation. This improvement means the results obtained using the model calculation become consistent with those obtained using the micromagnetic simulation.

In this study, we propose a new HAMR model calculation using the reversal probability of grain magnetization for each attempt. The required statistical thermal stability factor (TSF) is a function of the bit error rate (bER). Therefore, a previous model calculation using TSF can obtain the minimum  $K_u / K_{\text{bulk}}$  value for a given bER. A new model calculation can obtain the bER as a function of the writing field  $H_w$  for a given  $K_u / K_{\text{bulk}}$ . We discuss the physical implication of the recording time window using a new model calculation. The allowable ranges of  $H_w$  and  $K_u / K_{\text{bulk}}$  are also provided for various Curie temperatures.

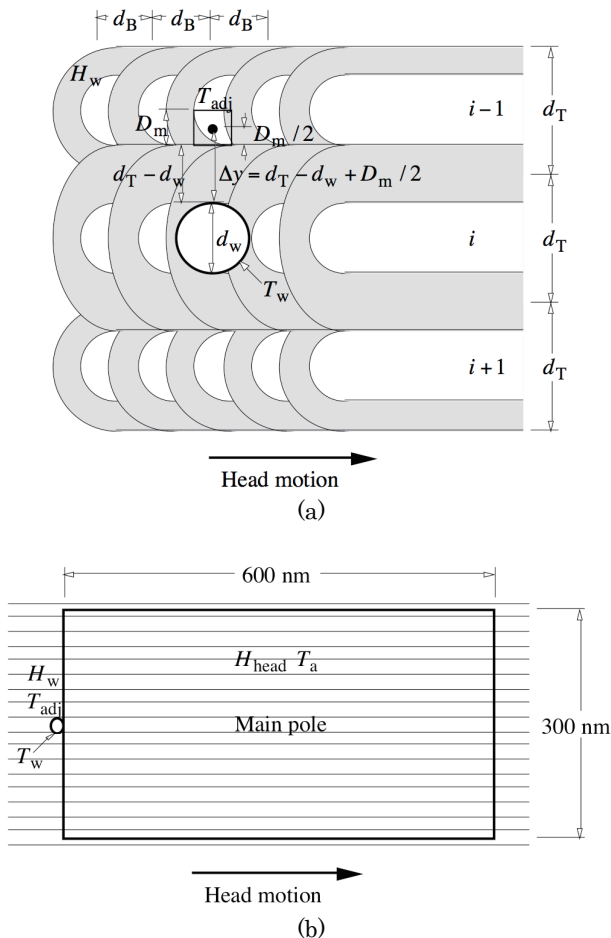
## 2. Calculation Conditions

### 2.1 Recording conditions

The medium was assumed to be granular. The arrangement of the grains was not considered. Figure 1 (a) is a schematic illustration of the area near the writing position for HAMR. The writing field  $H_w$  is

applied to a wide area including the writing position. The circle denoted the writing temperature  $T_w$  is an isotherm of  $T_w$ , and  $d_w$  is the heat-spot diameter.  $T_w$  is defined in 3.1. The white regions indicate upward or downward magnetization, and the gray regions indicate a magnetization transition that contains upward and downward magnetization grains. The transition region spreads to adjacent tracks as a result of rewriting operations on the  $i$ th track.  $T_{adj}$  is the maximum temperature at which information in adjacent tracks can be held during rewriting.  $\Delta y$  is the distance between  $T_w$  and  $T_{adj}$ , and was assumed to be  $d_T - d_w + D_m/2$ , where  $d_T$  is the track pitch and  $D_m$  is the mean grain size.  $d_B$  is the bit pitch.

Figure 1 (b) shows the writing-head configuration. We assume that the main-pole size of the head is 600 nm (down-track direction)  $\times$  300 nm (cross-track direction), and the writing position is located on the trailing side of the main pole.  $H_{head}$  is the maximum head field that can hold information under the main pole during rewriting. The maximum temperature under the main pole is  $T_a$ , which is the maximum ambient temperature of the hard drive, and is assumed to be 330 K.



**Fig. 1** Schematic illustrations of (a) writing position and (b) writing-head configuration.

**Table 1** Recording parameters and standard values.

User areal density (Tbpsi)	4
Bit area $S = d_B \times d_T$ (nm <sup>2</sup> )	140
Bit aspect ratio $d_T/d_B$	3
Heat-spot diameter $d_w$	$d_T/2$
Ambient temperature $T_a$ (K)	330
Linear velocity $v$ (m/s)	10

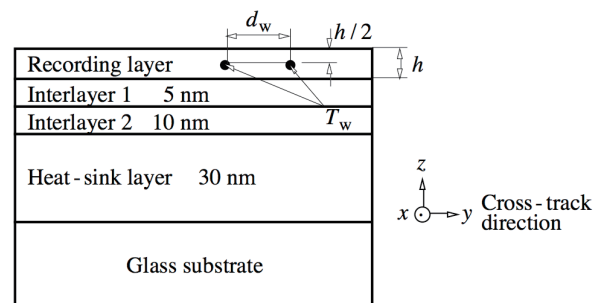
The recording parameters and the standard values are summarized in Table 1. The areal density calculated from the bit area  $S$  is 0.6 Tbpsi larger than the user areal density. The difference is the data for the error correction code and others.

$d_w = d_T/2$  is a design parameter, and is changed by the light power used for heating. If the light power alone is increased for a medium with the same Curie temperature  $T_c$ , the temperature profile increases and the written bits will be spread in the cross-track direction. Thus it becomes impossible to keep the track pitch constant. Therefore, we must adjust  $T_c$  to maintain  $d_w$  when we change the temperature profile by changing the light power.

## 2.2 Medium conditions

The standard medium structure is shown in Fig. 2. The standard medium consists of four layers, that is, a recording layer RL (Fe-Pt base, thickness  $h = 8$  nm), an interlayer 1 IL1 (MgO base, 5 nm), an interlayer 2 IL2 (Cr base, 10 nm), and a heat-sink layer HSL (Cu base, 30 nm). The  $x$ ,  $y$ , and  $z$  axes are the down-track, cross-track, and thickness directions, respectively.  $d_w$  is defined at the heat-spot edge and is at the center of the RL layer in the thickness direction. The two positions of  $T_w$  in Fig. 2 are at a distance of  $d_w$  in the cross-track direction as shown in Fig. 1 (a).

The medium parameters and the standard values are summarized in Table 2.  $D_m$  can be calculated from  $\sqrt{S/n} - \Delta$ , where  $n$  is the grain number per bit and  $\Delta$  is the non-magnetic spacing between grains.  $K_{um}$  is the mean anisotropy constant. The standard deviation of the Curie temperature  $\sigma_{Tc}$  is assumed to be zero.



**Fig. 2** Standard medium structure and definition of writing temperature  $T_w$ .

**Table 2** Medium parameters and standard values.

RL thickness $h$ (nm)	8
Non-magnetic spacing $\Delta$ (nm)	1
Grain number per bit $n$ (grain/bit)	4
Standard deviation of grain size $\sigma_D/D_m$ (%)	10
Standard deviation of anisotropy $\sigma_K/K_{um}$ (%)	0
Standard deviation of Curie temp. $\sigma_{T_c}/T_c$ (%)	0

The temperature dependence of the magnetization  $M_s$  was determined using a mean field analysis<sup>4)</sup>, and that of  $K_{um}$  was assumed to be proportional to  $M_s^2$ .  $T_c$  can be adjusted by the Cu simple dilution of  $(Fe_{0.5}Pt_{0.5})_{1-z}Cu_z$ .  $M_s(T_c, T)$  is a function of  $T_c$  and  $T$ , and  $M_s(T_c = 770 \text{ K}, T = 300 \text{ K}) = 1000 \text{ emu/cm}^3$  was assumed. On the other hand,  $K_{um}(T_c, K_u/K_{bulk}, T)$  is a function of  $T_c$ ,  $K_u/K_{bulk}$ , and  $T$ , and  $K_{um}(T_c = 770 \text{ K}, K_u/K_{bulk} = 1, T = 300 \text{ K}) = 70 \text{ Merg/cm}^3$  was assumed.  $K_u/K_{bulk}$  is the intrinsic ratio of medium  $K_u$  to bulk  $K_u$ . It is necessary to design a medium with a smaller  $K_u/K_{bulk}$  in terms of achieving good media productivity.

### 2.3 Heat-transfer calculation conditions

The heat-transfer calculation conditions including the thermal conductivities for each layer are the same as those reported in a previous paper<sup>4)</sup>.

The heat-transfer thermal gradients  $\partial T/\partial x$  for the down-track direction and  $\partial T/\partial y$  for the cross-track direction are calculated by a heat-transfer simulation.  $\partial T/\partial x$  and  $\partial T/\partial y$  for  $T_w = T_{wj}$  can be calculated using those for  $T_w = T_{wi}$  as

$$\frac{\partial T}{\partial x}(T_{wj}) = \frac{\partial T}{\partial x}(T_{wi}) \frac{T_{wj} - T_a}{T_{wi} - T_a} \quad \text{and} \quad (1)$$

$$\frac{\partial T}{\partial y}(T_{wj}) = \frac{\partial T}{\partial y}(T_{wi}) \frac{T_{wj} - T_a}{T_{wi} - T_a}, \quad (2)$$

respectively. Equations (1) and (2) are valid for  $T_c$  instead of  $T_w$  since  $T_w \approx T_c$ . It is important that the heat-transfer thermal gradient is simultaneously increased as  $T_w$  ( $T_c$ ) increases. Since  $\partial T/\partial x \approx \partial T/\partial y$ ,  $\partial T/\partial x = \partial T/\partial y$  is expressed as  $\partial T/\partial x(y)$  in the following.

**Table 3** Bit error rate calculation parameters and standard values.

Attempt frequency $f_0$ ( $s^{-1}$ )	$10^{11}$
(Attempt period $\tau_{AP}$ (ns))	0.01
Maximum rewriting number $N_{rew}$	$10^4$
Signal threshold	0.35
Bit error rate bER	$10^{-3}$

### 2.4 Bit error rate calculation conditions

The bit error rate (bER) calculation parameters and the standard values are summarized in Table 3.

The statistical thermal stability factor TSF is calculated statistically using many bits. Each bit has  $n$  grains, and the grains have various sizes  $D$  and anisotropy constants  $K_u$ .  $D$  (lognormal distribution) and  $K_u$  (normal distribution) are randomly generated by a computer. Each grain has the grain error probability  $P$

$$P = 1 - \exp\left(-f_0\tau \exp\left(-\text{TSF} \cdot \left(\frac{D}{D_m}\right)^2 \cdot \frac{K_u}{K_{um}}\right)\right), \quad (3)$$

where  $\tau$  is time. TSF is the thermal stability factor for  $D = D_m$  and  $K_u = K_{um}$ , and is unrelated to  $K_u$ . The bER is a function of  $P(\tau, \text{TSF})$ ,  $n$ ,  $\sigma_D$ , and  $\sigma_K$ . If the bER is fixed, TSF is a function of  $\tau$ ,  $n$ ,  $\sigma_D$ , and  $\sigma_K$ , that is,  $\text{TSF}(\tau, n, \sigma_D, \sigma_K)^{2, 3)}$ .

Errors occur in some grains of a bit. It is assumed that if the sum of the area with no error grains  $\Sigma D_i^2$  is 35 % larger than  $nD_m^2$  in one bit, the bit has no error. The maximum allowable bER is assumed to be  $10^{-3}$ .

## 3. Calculation Method

### 3.1 Reversal probability of grain magnetization

First, we explain the reversal probability of grain magnetization and the recording time window. The magnetization reversal number during  $\tau$  is given by

$$f_0\tau \exp(-K_\beta), \quad (4)$$

where  $K_\beta$  is the medium thermal stability factor. When  $\tau = \tau_{AP} = 1/f_0 = 10^{-11} \text{ s} = 0.01 \text{ ns}$ , Eq. (4) becomes

$$\exp(-K_\beta), \quad (5)$$

where  $\tau_{AP}$  is the attempt period. Equation (5) is the reversal probability of grain magnetization for each attempt. For example, when  $K_\beta = 0$ ,  $\exp(-K_\beta)$  becomes one, where  $M_s$  reversal always occurs for each attempt.  $K_{\beta+}$  where  $M_s$  is parallel to the writing field  $H_w$ , and  $K_{\beta-}$  where  $M_s$  is antiparallel to  $H_w$  are expressed by

$$K_{\beta+}(T, H_w) = \frac{K_u(T)V}{kT} \left(1 + \frac{H_w}{H_c(T)}\right)^2, \quad (6)$$

and

$$K_{\beta-}(T, H_w) = \frac{K_u(T)V}{kT} \left(1 - \frac{H_w}{H_c(T)}\right)^2 \quad (H_w \leq H_c(T)),$$

$$K_{\beta-}(T, H_w) = 0 \quad (H_c(T) < H_w), \quad (7)$$



respectively, where  $H_c$  is the coercivity. Therefore, the probability  $p_+$  for each attempt where  $M_s$  and  $H_w$  change from parallel to antiparallel is expressed by

$$p_+ = \exp(-K_{\beta+}). \quad (8)$$

On the other hand,

$$p_- = \exp(-K_{\beta-}) \quad (9)$$

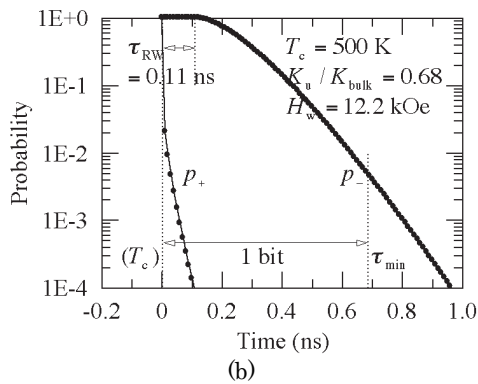
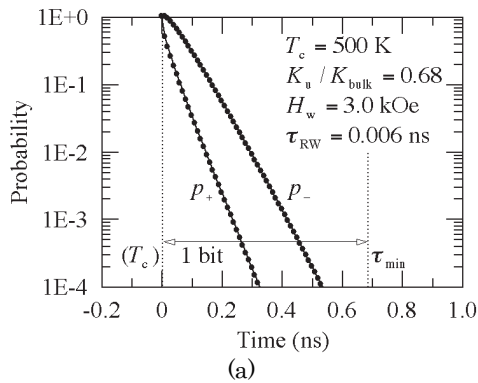
is the probability for each attempt where  $M_s$  and  $H_w$  change from antiparallel to parallel.

In this paper, the recording time window  $\tau_{RW}$  is defined by

$$\tau_{RW} = \frac{T_c - T_w}{(\partial T / \partial x) \cdot v}, \quad (10)$$

where  $v$  is the linear velocity. Since  $v = \partial x / \partial t$ ,  $(\partial T / \partial x) \cdot v$  is the cooling rate  $\partial T / \partial t$ . Therefore,  $\tau_{RW}$  is the cooling time from  $T_c$  to  $T_w$ . And then, the relationship between  $H_w$  and  $T_w$  is defined by

$$H_w = H_{cm}(T_c, K_u / K_{bulk}, T_w) = \frac{2K_{um}(T_c, K_u / K_{bulk}, T_w)}{M_s(T_c, T_w)}, \quad (11)$$

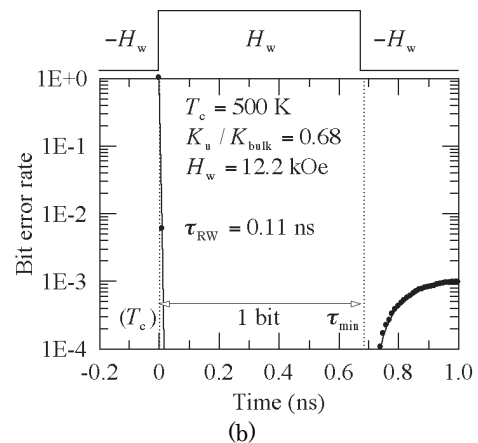
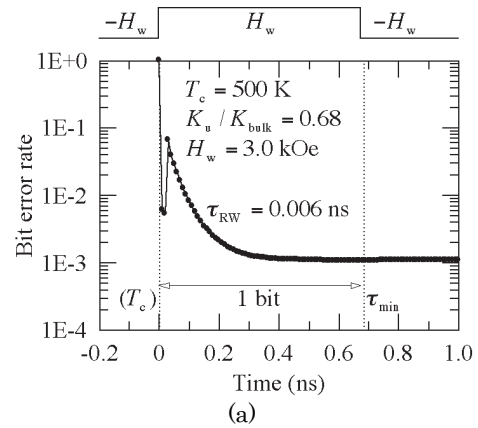


**Fig. 3** Dependence of reversal probability of grain magnetization on time for (a) writing field  $H_w = 3.0$  kOe and (b) 12.2 kOe.

where  $H_{cm}$  is the mean coercivity. The media can be designated by  $T_c$  and  $K_u / K_{bulk}$ . On the other hand,  $\tau_{RW}$  is a function of  $T_c$ ,  $K_u / K_{bulk}$ ,  $\partial T / \partial x$ ,  $v$  and  $H_w$  since  $T_w$  is a function of  $T_c$ ,  $K_u / K_{bulk}$  and  $H_w$ .

Figure 3 shows the dependence of the reversal probability of grain magnetization on time. The time corresponding to  $T_c$  is 0 ns, and the minimum magnetization transition window  $\tau_{min} = d_B / v$  corresponding to 1 bit is 0.68 ns since  $d_B$  is 6.8 nm and  $v$  is 10 m/s. The time after  $\tau_{min}$  corresponds to the next bit. The filled circles are the probabilities for each attempt. The  $p_+$  and  $p_-$  values are both one at 0 ns since  $K_{\beta\pm} = 0$ .  $p_-$  is always equal to one during  $\tau_{RW}$ . A lower  $p_+$  and a higher  $p_-$  are better between 0 and  $\tau_{min}$  in terms of stable writing, and lower  $p_+$  and  $p_-$  values are both better after  $\tau_{min}$  in terms of information (written bit) stability.

Figure 3 (a) shows the result when  $T_c = 500$  K,  $K_u / K_{bulk} = 0.68$  and  $H_w$  is low ( $= 3.0$  kOe). The resulting  $\tau_{RW}$  value is 0.006 ns, and  $\tau_{RW}$  is too short.  $p_-$  is rapidly decreased after 0 ns and  $p_+$  is not sufficiently low before  $\tau_{min}$ , which is not suitable for stable writing. This corresponds to write-error (WE).



**Fig. 4** Dependence of bit error rate on time for (a) writing field  $H_w = 3.0$  kOe and (b) 12.2 kOe.

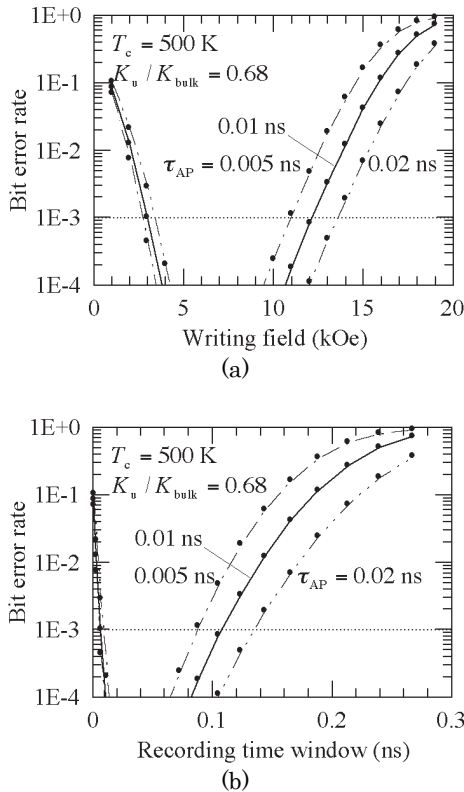
Figure 3 (b) shows the result when  $T_c = 500$  K,  $K_u / K_{bulk} = 0.68$  and  $H_w$  is high ( $= 12.2$  kOe). The

resulting  $\tau_{RW}$  value is 0.11 ns, and  $\tau_{RW}$  is too long. In this case,  $p_-$  is sufficiently high and  $p_+$  is sufficiently low before  $\tau_{RW}$ . Therefore, low WE can be expected. However,  $p_-$  has a relatively large value after  $\tau_{min}$  corresponding to the next bit, which is unsuitable as regards the information stability at the next bit when the direction of  $H_w$  is changed after  $\tau_{min}$ . This corresponds to erasure-after-write (EAW).

### 3.2 Bit error rate calculation

The bER can be calculated by the Monte Carlo method using the reversal probability of grain magnetization  $p_{\pm}$  for each attempt period. First, the medium is determined by  $T_c$  and  $K_u/K_{bulk}$ . The grain temperature falls from  $T_c$  according to  $\partial T/\partial x$  and  $v$  during the writing process. The magnetic property and then  $p_{\pm}$  are calculated by employing a mean field analysis for each attempt period. The magnetization direction can be determined by the Monte Carlo method for each attempt period. The bER is obtained from the mean of  $10^6$  bits since the results are scattered.

Figure 4 (a) shows the bER dependence on time for the same conditions shown in Fig. 3 (a). The direction of  $H_w$  is changed after  $\tau_{min}$  to examine the EAW. The bER remains high before  $\tau_{min}$  since  $H_w$  is too low, that is, WE. A case where  $H_w$  is too high is shown in Fig. 4 (b), which corresponds to Fig. 3 (b). Although the bER is sufficiently low before  $\tau_{min}$ , it increases after  $\tau_{min}$ , that is, EAW.



**Fig. 5** Dependence of bit error rate on (a) writing field and (b) recording time window for various attempt periods  $\tau_{AP}$ .

### 3.3 Attempt period

The attempt period is an uncertain parameter. Figure 5 shows the bER dependence on (a)  $H_w$  and (b)  $\tau_{RW}$  for various attempt periods  $\tau_{AP}$ . A high bER in a low  $H_w$  (a short  $\tau_{RW}$ ) range is caused by WE, and that in a high  $H_w$  (a long  $\tau_{RW}$ ) range is caused by EAW. The overall tendencies of bER are not greatly changed by doubling  $\tau_{AP}$ .

### 3.4 HAMR conditions

Five HAMR conditions are examined to estimate the allowable ranges of  $H_w$  and  $K_u/K_{bulk}$ .

Condition I is the information stability during 10 years of archiving. The minimum  $K_u/K_{bulk}$  value can be calculated using a previous model calculation<sup>4</sup> by solving

$$\frac{K_{um}(T_c, K_u/K_{bulk}, T_a)V_m}{kT_a} = \text{TSF}_{10} \equiv \text{TSF}(10 \text{ years}, n, \sigma_D, \sigma_K), \quad (12)$$

where  $V_m$  is the grain volume for mean grain size.

Condition II is the restriction of WE. The minimum  $H_w$  value for WE can be calculated using the new model calculation mentioned in 3.2.

Condition III is the restriction of EAW. The maximum  $H_w$  value for EAW can also be calculated using the new model calculation mentioned in 3.2.

Condition IV is the information stability in adjacent tracks during rewriting, that is, adjacent-track-interference (ATI). The maximum  $H_w$  value for ATI can be calculated by solving

$$K_{\beta-}(T_{adj}, H_w) = \text{TSF}_{adj} \equiv \text{TSF}\left(\frac{d_B}{v} \times N_{rew}, n, \sigma_D, \sigma_K\right) \quad (13)$$

(thermal stability condition)<sup>5</sup>,

$$\frac{T_w(H_w) - T_{adj}}{\Delta y} = \frac{\partial T}{\partial y} \quad (14)$$

(thermal gradient condition)<sup>5</sup>, and Eq. (11).

Condition V is the information stability under the main pole during rewriting. The maximum  $H_{head}$  value can be calculated using a previous model calculation<sup>5</sup> by

$$H_{head} = H_{cm}(T_a) \left(1 - \sqrt{\frac{\text{TSF}_{head}}{K_{um}(T_a)V_m/(kT_a)}}\right), \quad (15)$$

where

$$\text{TSF}_{head} \equiv \text{TSF}(\tau_{head} \times N_{rew} \times (N_T - 1), n, \sigma_D, \sigma_K), \quad (16)$$

$\tau_{head} = 600 \text{ nm}/v$ , and  $N_T = 300 \text{ nm}/d_T$ .

4. Calculation Results

4.1 Heat-transfer thermal gradient

$\tau_{RW}$  is a function of  $T_c$ ,  $K_u/K_{bulk}$ ,  $\partial T/\partial x$ ,  $v$  and  $H_w$ . First, we examine the relationship between  $\tau_{RW}$  and  $\partial T/\partial x$ . Figure 6 shows the dependence of bER on (a)  $H_w$  and (b)  $\tau_{RW}$  for various  $\partial T/\partial x$  values. Open circles indicate the bER for EAW when  $\tau_{RW} = 0.1$  ns. As shown in Fig. 6 (b), although the bER values for WE in a short  $\tau_{RW}$  range ( $< 0.02$  ns) are almost the same for various  $\partial T/\partial x$  values, the bER for EAW at  $\tau_{RW} = 0.1$  ns for  $\partial T/\partial x = 4.9$  K/nm is higher than that for 6.9 K/nm.

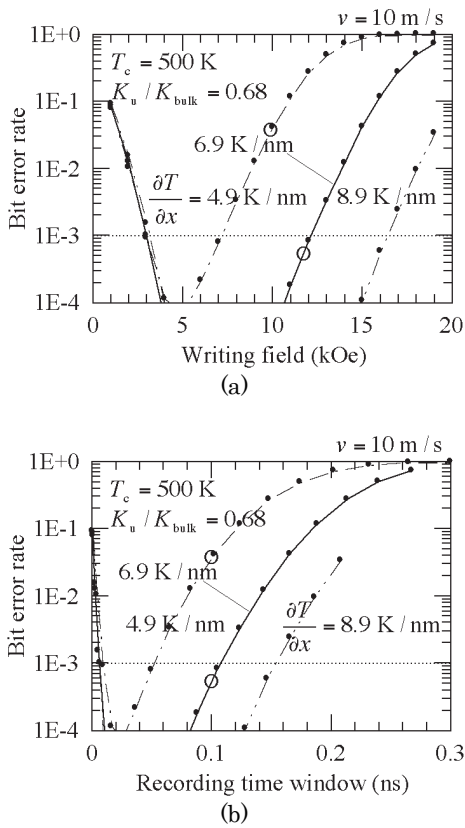


Fig. 6 Dependence of bit error rate on (a) writing field and (b) recording time window for various heat-transfer thermal gradients  $\partial T/\partial x$ .

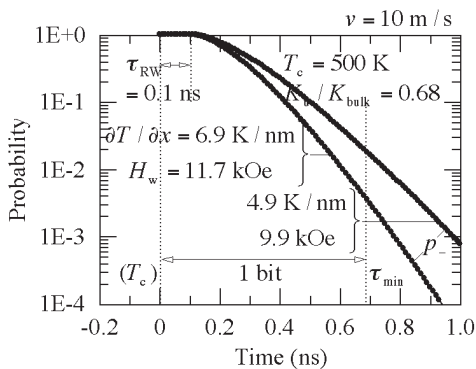


Fig. 7 Dependence of reversal probability of grain magnetization on time for heat-transfer thermal gradients  $\partial T/\partial x = 4.9$  K/nm and 8.9 K/nm.

This difference can be explained using Fig. 7. The bER for EAW is determined by  $p_-$  after  $\tau_{min}$ . Although the  $\tau_{RW}$  values are the same, the  $p_-$  values after  $\tau_{min}$  are different since the  $\partial T/\partial x$  values are different. Although  $\tau_{RW}$  is a good guideline for WE and EAW when  $\partial T/\partial x$  is constant as shown in Figs. 3 and 4, EAW cannot be determined solely by  $\tau_{RW}$  as shown in Figs. 6 and 7 when  $\partial T/\partial x$  changes.

4.2 Linear velocity

Next, we examine the relationship between  $\tau_{RW}$  and  $v$ . Figure 8 shows the dependence of bER on (a)  $H_w$  and (b)  $\tau_{RW}$  for various  $v$  values. Open circles also indicate the bER for EAW when  $\tau_{RW} = 0.1$  ns. The bER at  $\tau_{RW} = 0.1$  ns for  $v = 20$  m/s is higher than that for 10 m/s as shown in Fig. 8 (b). This difference can be explained using Fig. 9. Since Fig. 9 (a) and (b) show the case where  $v = 10$  m/s and 20 m/s, respectively, the  $\tau_{min}$  values are 0.68 ns and 0.34 ns for Fig. 9 (a) and (b), respectively. The bER for EAW is determined by  $p_-$  after  $\tau_{min}$ . Since the ratios of  $\tau_{RW}$  to  $\tau_{min}$  are 14.6 % and 29.3 % for Fig. 9 (a) and (b), respectively, the  $p_-$  value after  $\tau_{min}$  for  $v = 20$  m/s is higher than that for  $v = 10$  m/s. Therefore, the bER for EAW at  $\tau_{RW} = 0.1$  ns for  $v = 20$  m/s becomes higher than that for  $v = 10$  m/s. EAW cannot be determined solely by  $\tau_{RW}$  as shown in Figs. 8 and 9 when  $v$  changes.

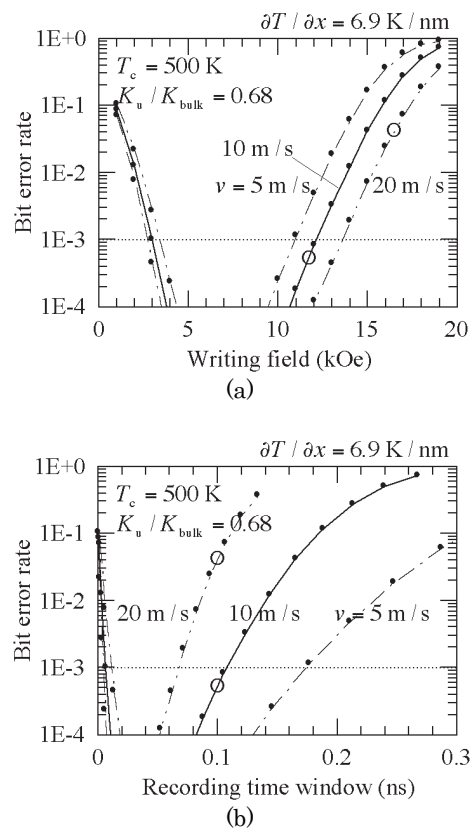
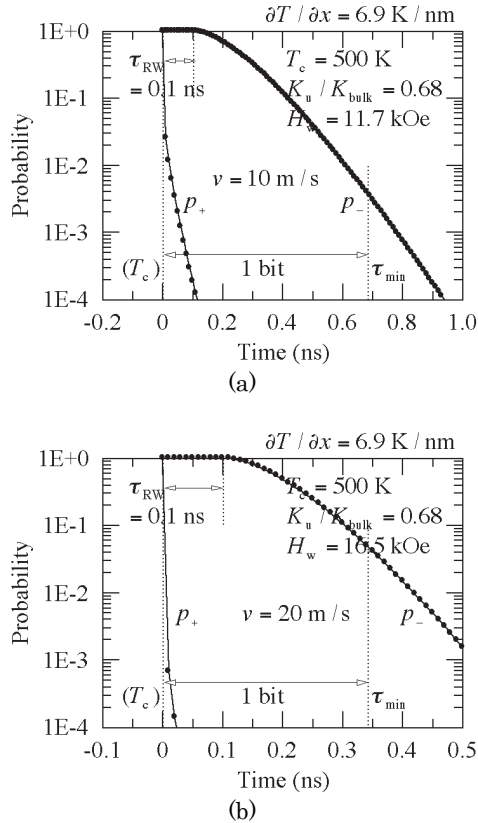
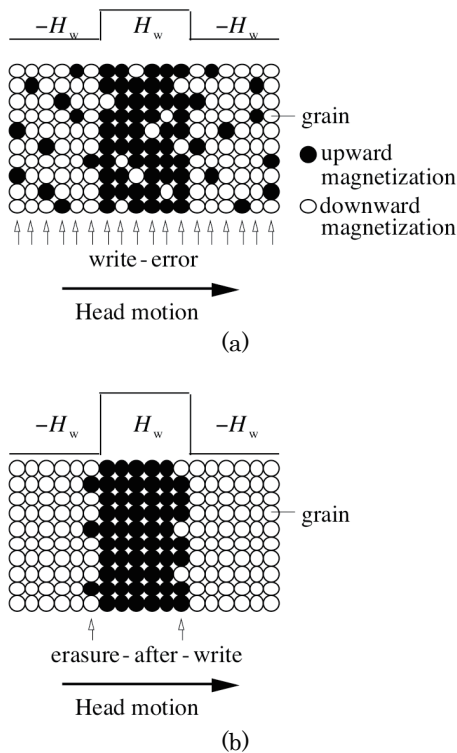


Fig. 8 Dependence of bit error rate on (a) writing field and (b) recording time window for various linear velocities  $v$ .



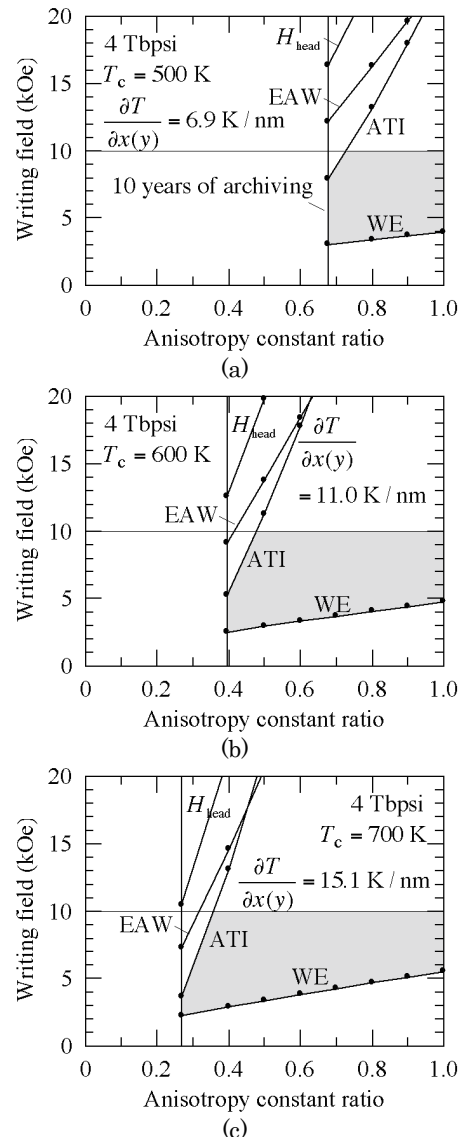


**Fig. 9** Dependence of reversal probability of grain magnetization on time for (a) linear velocities  $v = 10$  m/s and (b) 20 m/s.



**Fig. 10** Schematic illustrations of (a) write-error and (b) erasure-after-write.

Figure 10 shows a schematic illustration of (a) WE and (b) EAW where the bit and the track pitches are much longer than those of this calculation. WE occurs in every grain column during writing as shown in Fig. 10 (a) considering Fig. 4 (a) when  $H_w$  is too low. On the other hand, EAW occurs at one or two columns of grains on just the former bit edge as shown in Fig. 10 (b) considering Fig. 4 (b) when  $H_w$  is too high. Although WE is independent of bit pitch, the influence of EAW depends on bit pitch, and when the bit pitch is long, it is difficult to examine the influence of EAW. Since the bit pitch is short in this calculation, the influence of EAW can be accurately examined, and EAW will be important for the density of 4 Tbps.



**Fig. 11** Allowable range of writing field and anisotropy constant ratio for (a) Curie temperatures  $T_c = 500$  K, (b) 600 K, and (c) 700 K where WE, EAW, ATI, and  $H_{head}$  are write-error, erasure-after-write, adjacent-track-interference, and the maximum head field under the main pole, respectively.

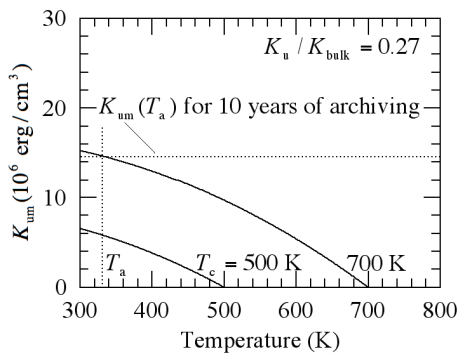
**4.3 Allowable range**

This model calculation can estimate the allowable range of  $H_w$  and  $K_u/K_{bulk}$ .

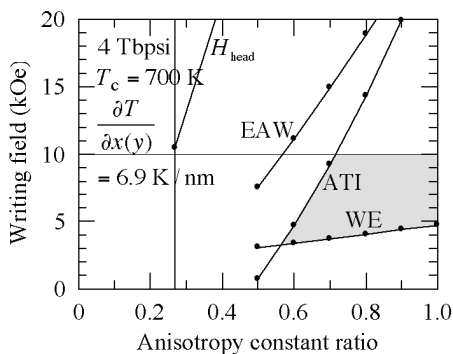
In Fig. 11, condition I (10 years of archiving) determines the minimum  $K_u/K_{bulk}$  value, and condition II (WE) determines the minimum  $H_w$  value. The maximum  $H_w$  value is determined from condition III (EAW), condition IV (ATI), and condition V ( $H_{head}$ ) as mentioned in 3.4. The maximum  $H_w$  value that the writing head can supply was assumed to be 10 kOe. As a result, the gray regions indicate the allowable range. The limiting factors are 10 years of archiving, WE, and ATI in this calculation.

$\partial T/\partial x(y)$  is simultaneously increased as  $T_c$  increases in Fig. 11 (a), (b), and (c) as mentioned in 2.3. The minimum  $K_u/K_{bulk}$  value (10 years of archiving) becomes low as  $T_c$  increases, and then the allowable range widens as  $T_c$  increases.

The reason for the shift of the minimum  $K_u/K_{bulk}$  value (10 years of archiving) can be explained using the temperature dependence of  $K_{um}$  as shown in Fig. 12 where the  $K_u/K_{bulk}$  values are the same. The rates at which  $K_u$  increase ( $\partial K_u/\partial T$ ) are almost the same.  $K_{um}$  at  $T_a$  for  $T_c = 500$  K is insufficient for 10 years of archiving since the temperature difference between  $T_c$  and  $T_a$  is small. On the other hand,  $K_{um}$  at  $T_a$  for  $T_c = 700$  K is sufficient. Therefore, the small  $K_u/K_{bulk}$  value becomes allowable as  $T_c$  increases.



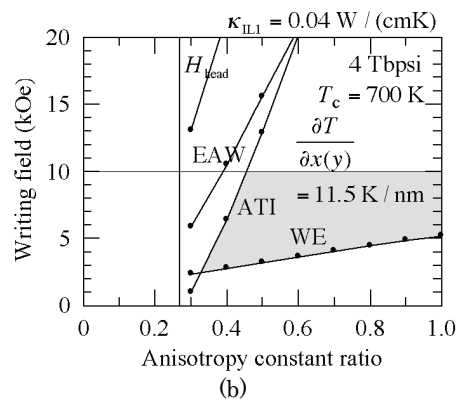
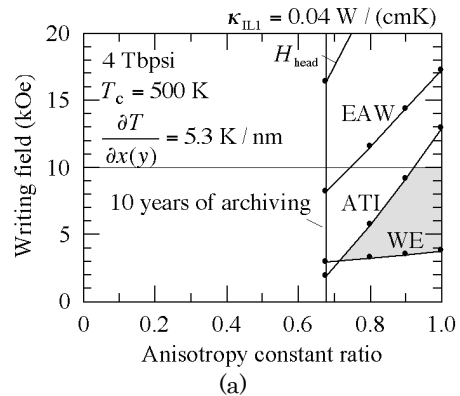
**Fig. 12** Dependence of mean anisotropy constant  $K_{um}$  on temperature for Curie temperatures  $T_c = 500$  K and 700 K.



**Fig. 13** Allowable range of writing field and anisotropy constant ratio for Curie temperature  $T_c = 700$  K and heat-transfer thermal gradient  $\partial T/\partial x(y) = 6.9$  K/nm.

Another reason for widening the allowable range is the increase in  $\partial T/\partial x(y)$ , that is,  $\partial T/\partial x(y)$  is simultaneously increased as  $T_c$  increases as mentioned in 2.3. Figure 13 shows the allowable range for  $T_c = 700$  K when  $\partial T/\partial x(y)$  is 6.9 K/nm instead of 15.1 K/nm (Fig. 11 (c)). The maximum  $H_w$  value restricted by EAW and ATI, which are closely related to  $\partial T/\partial x(y)$ , is greatly decreased from Fig. 11 (c). If  $\partial T/\partial x(y)$  is not simultaneously increased, the overall tendency of the allowable range is not greatly changed by increasing  $T_c$  when we compare Fig. 11 (a) and Fig. 13.

Figure 14 shows the allowable range calculated using the thermal conductivity of interlayer 1  $\kappa_{IL1} = 0.04$  W/(cmK) reported for sputtered MgO film<sup>10</sup> instead of the standard value of 0.5 W/(cmK)<sup>4</sup>.  $\partial T/\partial x(y)$  is decreased from 6.9 K/nm (Fig. 11 (a)) to 5.3 K/nm (Fig. 14 (a)) for  $T_c = 500$  K. Then, the allowable range is greatly decreased. Since the allowable range is sensitive to  $\partial T/\partial x(y)$ , the thermal conductivity is an important design parameter.



**Fig. 14** Allowable range of writing field and anisotropy constant ratio for (a) Curie temperatures  $T_c = 500$  K and (b) 700 K when the thermal conductivity of interlayer 1  $\kappa_{IL1}$  is 0.04 W/(cmK).

**5. Conclusions**

We propose a new model calculation using the reversal probability of grain magnetization for heat-assisted magnetic recording. The physical implication of the recording time window  $\tau_{RW}$

proposed in the micromagnetic calculation is discussed using a new model calculation. Although  $\tau_{RW}$  is a good guideline for write-error and erasure-after-write (EAW), EAW cannot be determined solely by  $\tau_{RW}$ . The influence of EAW is accurately examined, and EAW will be important for the density of 4 Tbps.

The allowable range of the writing field and the anisotropy constant ratio  $K_u/K_{\text{bulk}}$  is also provided for various Curie temperatures  $T_c$ . The allowable range widens as  $T_c$  increases. The reasons for this are the temperature difference between  $T_c$  and the ambient temperature, and the simultaneous increase in the heat-transfer thermal gradient  $\partial T/\partial x(y)$  as  $T_c$  increases.  $T_c$  and  $\partial T/\partial x(y)$  are important parameters for reducing  $K_u/K_{\text{bulk}}$ .

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# Optimum preparation conditions of Fe-deficient Ca-based M-type ferrite

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We investigated synthesis conditions and magnetic properties of Fe-deficient Ca-based hexagonal ferrites,  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_y\text{O}_{19-o}$  ( $x = 0.1-0.3$ ,  $y = 2.0-10$ ), and found the formation of M-type ferrite at  $x = 0.1-0.3$  and  $y = 7.0-9.0$  above  $1200^\circ\text{C}$ . Samples of  $y = 2.0-6.0$  showed deviation from the initial compositions since molten calcium-rich oxide (possibly  $\text{CaFe}_2\text{O}_4$ ) leaked out from the samples above  $1200^\circ\text{C}$ . The X-ray diffraction pattern of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-o}$  sintered at  $1250^\circ\text{C}$  demonstrates the single phase of M-type hexagonal ferrite. The saturation magnetization of this sample was  $68.0 \text{ Am}^2/\text{kg}$  at room temperature and its Curie temperature was about  $400^\circ\text{C}$ , which is slightly lower than that of the Sr-based M-type ferrite ( $460^\circ\text{C}$ ).

**Keywords:** hexagonal ferrites, M-type, calcium compound

## 1. Introduction

M-type ferrite is a type of hexagonal ferrite. Its chemical formula is expressed as  $\text{M}^{2+}\text{Fe}^{3+}_{12}\text{O}_{19}$  ( $\text{M}^{2+}=\text{Ba}^{2+}, \text{Sr}^{2+}$ ). The M-type ferrite has high saturation magnetization and high coercivity and is mainly used as a permanent magnet. The Curie temperatures of  $\text{BaFe}_{12}\text{O}_{19}$  and  $\text{SrFe}_{12}\text{O}_{19}$  are  $450^\circ\text{C}$  and  $460^\circ\text{C}$ , respectively.<sup>1)-4)</sup>

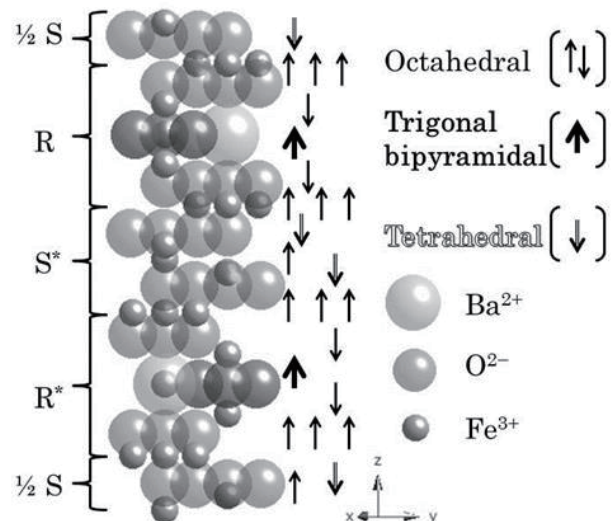
The unit cell of M-type ferrite is composed of two kinds of block units, where a R-block and a S-block are stacked up alternately (RSR\*S\*). The symbol \* means  $180^\circ$  rotation of the corresponding block around the  $c$ -axis.<sup>1), 3), 4)</sup> The M-type ferrite has ions of  $2(\text{MFe}_{12}\text{O}_{19})$  in the unit cell (RSR\*S\*), as shown in Fig. 1.

The S-block with the chemical formula of  $(2\text{Fe}_3\text{O}_4)^{2+}$  is identical to the cubic spinel structure. Two close-packed large oxygen anion layers (O layers) build the framework of the S-block. One octahedral (up-spin) and two tetrahedral (down-spin) sites exist for small  $\text{Fe}^{3+}$  cations in the S-block.<sup>1), 3), 4)</sup>

The R-block contains another kind of close-packed large ion layer with  $\text{M}^{2+}:\text{O}^{2-} = 1:3$  (M-O layers). The R-block with the chemical formula of  $(\text{MFe}_6\text{O}_{11})^{2-}$  is made up of three large-ion layers where one M-O layer is sandwiched between two O layers. A trigonal-bipyramidal (up-spin) site is just on the M-O layer in the R-block. Two octahedral (down-spin) sites are between the M-O and O layers in the R-block. There are three octahedral (up-spin) sites just on the block border between the S- and R-blocks.<sup>1), 3), 4)</sup>

Because an  $\text{Fe}^{3+}$  ion has the magnetic moment of  $5 \mu_B$ , the total magnetization at zero temperature can be estimated from the numbers of the up and down spins with the assumption of a collinear magnetic structure. Typical M-type ferrite has eight up spins and four down spins as shown in Fig. 1. Hence, the net magnetization per formula unit is  $(8-4) \times (5 \mu_B) = 20 \mu_B$ .<sup>1), 4)</sup>

In this study, we investigated the synthesis conditions



**Fig. 1** Spin alignment in the unit cell of the M-type ferrite.

of Ca-based M-type ferrites. Ca is one of the alkaline earth elements. It is attractive to substitute Ca ions for Ba or Sr ions in the hexagonal ferrite because Ca is rich in resources.<sup>5)</sup> Also, the use of Ca, which is less toxic than Ba, is helpful in terms of producing a safer material.

The synthesis of Ca-based hexagonal ferrites is, however, extremely difficult because the M-type composition sample with  $\text{Ca}:\text{Fe} = 1:12$  tends to melt and decompose into  $\alpha\text{-Fe}_2\text{O}_3$ ,  $\text{CaFe}_4\text{O}_7$ , and  $\text{CaFe}_2\text{O}_4$ .<sup>6)-8)</sup>

On the other hand, the Ca-based M-type hexaferrite can be synthesized by adding a small amount of La in oxygen atmosphere.<sup>9), 10)</sup> This Ca-based M-type ferrite exists as a ternary oxide of  $\text{CaO-La}_2\text{O}_3\text{-Fe}_2\text{O}_3$  because there is no M-type  $\text{CaFe}_{12}\text{O}_{19}$  in the binary  $\text{CaO-Fe}_2\text{O}_3$  phase diagram as mentioned above. Most of the previous studies, however, treated  $\text{La}_2\text{O}_3$  as an additive



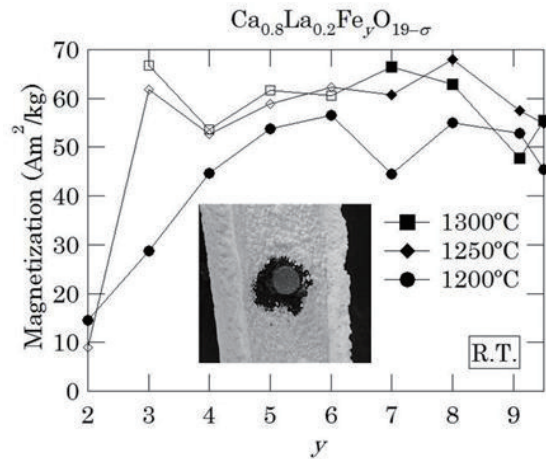
to  $\text{CaFe}_{12}\text{O}_{19}$ .<sup>9)-12)</sup> The systematic research was limited at ratio of  $\text{Fe}/(\text{Ca}+\text{La}) > 10$  although Fang reported that they obtained the M-type phase by reducing the amount of Fe.<sup>13)</sup> So, the synthesis conditions in air remain unclear. The synthesis condition of the Ca-based M-type ferrite was not systematically surveyed below  $\text{Fe}/(\text{Ca}+\text{La}) = 9$ . Therefore, we studied three synthesis conditions: the composition ratio of Ca:La, the ratio of (Ca+La):Fe, and the sintering temperature.

## 2. Experimental Procedure

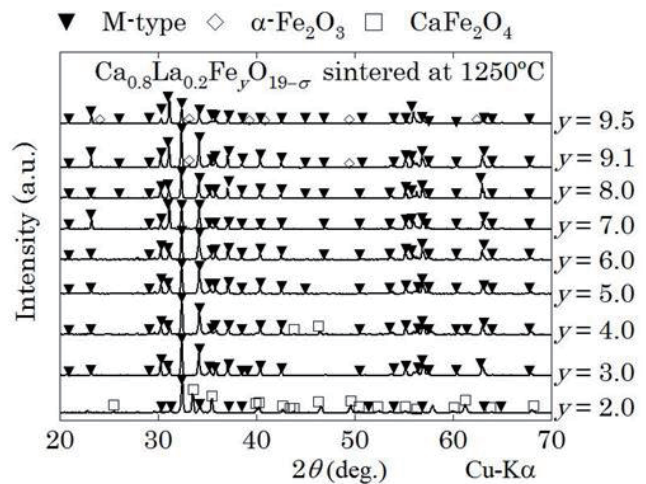
Samples of Ca-based M-type ferrite were prepared by a conventional ceramic method. We used  $\text{CaCO}_3$ ,  $\text{La}_2\text{O}_3$ , and  $\alpha\text{-Fe}_2\text{O}_3$  as starting materials. They were mixed in a desired proportion,  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_y\text{O}_{19-\sigma}$  ( $x = 0.1-0.3$ ,  $y = 2.0-10$ ). The powder was ball-milled for 24 h. The mixed powder was pressed into a pellet shape and pre-calcined in air at  $900^\circ\text{C}$ . The sintered sample was pulverized in a mortar and then milled into fine powder with a planetary ball mill (Fritsch, P-7 Premium line with 1 mm $\phi$  zirconia balls and a 45 ml zirconia container) for 10 min. at 1100 rpm. The processed powder was dried and then pressed into disks. The disks were sintered at 1100 to  $1300^\circ\text{C}$  for 5 h. Parts of some sintered samples at  $y \leq 6$  were molten above  $1250^\circ\text{C}$ . We removed the molten portion adhering to the pellet and employed the remaining part as a sample for measurements. The crystal structure of the sample was examined by powder X-ray diffraction (XRD) analysis with Cu-K $\alpha$  radiation. The magnetization was measured with a vibrating sample magnetometer (Tamakawa TM-VSM2130HGC) and a superconducting quantum interference device (SQUID) magnetometer (Quantum Design MPMS-XL). The composition was analyzed by the use of an Electron Probe Micro Analyzer (EPMA) (JEOL, JXA-8200). Here, the composition of oxygen was not examined because the analyses of light elements are less accurate than those of heavy elements.

## 3. Results and discussion

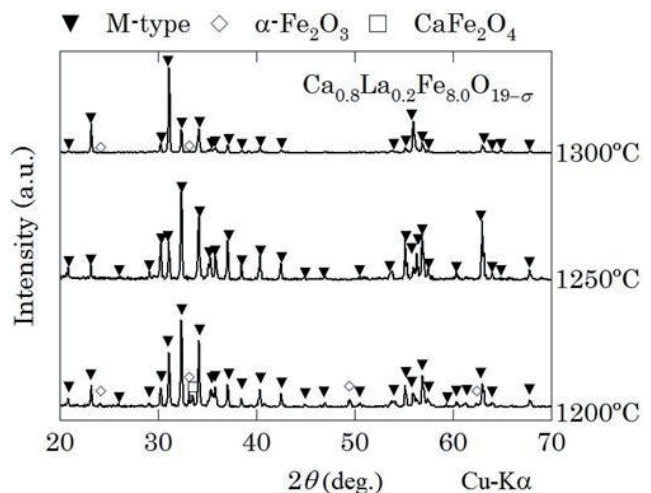
Figure 2 shows the room-temperature saturation magnetization of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_y\text{O}_{19-\sigma}$  ( $y = 2.0-9.5$ ) sintered at  $1200-1300^\circ\text{C}$ . The saturation magnetization was high for the samples sintered above  $1250^\circ\text{C}$  with  $y = 3.0-8.0$ . However, deviations from the initial compositions seems to take place below  $y = 6.0$  because molten oxides separated out from these initially poor-iron samples, as shown in the inset of Fig. 2. Actually, the EPMA measurement of the sample with the initial composition of  $y = 4.0$  sintered at  $1250^\circ\text{C}$  showed the average atomic ratio of Ca:La:Fe = 0.76:0.24:8.53, demonstrating a great deviation from the initial composition. The composition of the molten oxides is possibly close to Ca:Fe = 1:2 because  $\text{CaFe}_2\text{O}_4$  has the lowest melting point of  $1216^\circ\text{C}$  in the CaO- $\text{Fe}_2\text{O}_3$  system.<sup>6)-8)</sup> The maximum saturation magnetization is  $68.0 \text{ Am}^2/\text{kg}$  for the sample with the



**Fig. 2** Saturation magnetization at room temperature of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_y\text{O}_{19-\sigma}$  ( $y = 2.0-9.5$ ) sintered at  $1200$ ,  $1250^\circ\text{C}$  and  $1300^\circ\text{C}$ . Open markers indicate the samples whose molten portion was removed.



**Fig. 3** X-ray diffraction patterns of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_y\text{O}_{19-\sigma}$  ( $y = 2.0-9.5$ ) sintered at  $1250^\circ\text{C}$ .



**Fig. 4** X-ray diffraction patterns of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at  $1200^\circ\text{C}$ ,  $1250^\circ\text{C}$ , and  $1300^\circ\text{C}$ .

initial composition of Ca:La:Fe = 0.8:0.2:8.0 sintered at 1250°C.

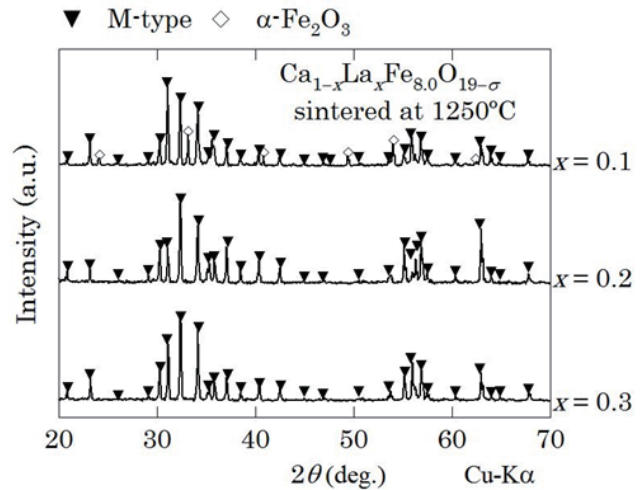
Figure 3 shows the X-ray diffraction patterns of the samples with the initial compositions of Ca:La:Fe = 0.8:0.2:y ( $y = 2.0-9.5$ ) sintered at 1250°C. The main phase is M-type ferrite for the samples with  $y \geq 3.0$ .<sup>14), 15)</sup> However, the compositions of the samples with  $y \leq 6.0$  are different from the initial compositions because molten calcium-rich oxide (possibly  $\text{CaFe}_2\text{O}_4$ ) was separated out from the samples sintered at  $T \geq 1250^\circ\text{C}$ . Also, there are minor  $\alpha\text{-Fe}_2\text{O}_3$  peaks in the X-ray diffraction patterns of the samples with  $y \geq 9.1$ . Therefore, the initial composition of  $y = 7.0$  or 8.0 is suitable for the preparation of Ca-based M-type ferrite.

Figure 4 shows the X-ray diffraction patterns of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at 1200°C, 1250°C, and 1300°C. The main phase of these samples is M-type ferrite. However, the sample sintered at 1200°C also has the secondary phases of  $\text{CaFe}_2\text{O}_4$  and  $\alpha\text{-Fe}_2\text{O}_3$ . Since the raw material of  $\alpha\text{-Fe}_2\text{O}_3$  remains, the sintering temperature of 1200°C is still insufficient for the formation of Ca-based M-type phase. On the other hand, if the sintering temperature was higher than 1300°C, the separation of molten oxides also took place, similar to that shown in the inset of Fig. 2. Therefore, the sintering temperature of about 1250°C is suitable for the preparation of Ca-based M-type ferrite.

Figure 5 shows the X-ray diffraction patterns of  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_{8.0}\text{O}_{19-\sigma}$  ( $x = 0.1-0.3$ ) sintered at 1250°C. The samples of  $x = 0.2$  and 0.3 have the single phase of M-type ferrite, but the sample of  $x = 0.1$  has the mixed phases of M-type and  $\alpha\text{-Fe}_2\text{O}_3$ . The raw material of  $\alpha\text{-Fe}_2\text{O}_3$  remains in the Ca-rich sample with  $x < 0.2$ . The lattice constants of these samples are shown in Table 1. The lattice constants of samples are close to those of SrM. On the other hand, the  $c$ -axis lattice constants are smaller than that of BaM. This is caused by the difference in the ionic radii because the ionic radii of  $\text{Ca}^{2+}$ ,  $\text{La}^{3+}$ ,  $\text{Sr}^{2+}$ , and  $\text{Ba}^{2+}$  are 1.12 Å, 1.16 Å, 1.26 Å, and 1.42 Å, respectively.<sup>16)</sup> The Ba cations with the large ionic radius may expand the  $c$ -axis of the BaM ferrite.

Figure 6 shows the temperature dependence of magnetization of  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_{8.0}\text{O}_{19-\sigma}$  ( $x = 0.1-0.3$ ) sintered at 1250°C. The Curie temperatures of these samples were about 400°C, which is slightly lower than that of the Sr-based M-type ferrite (460°C).<sup>2)</sup>

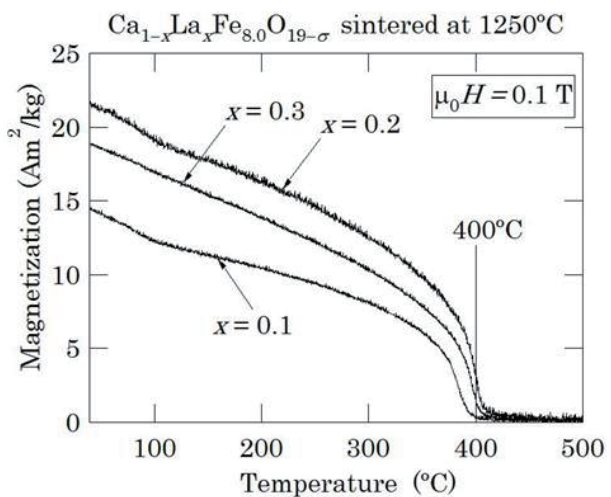
Table 2 shows the experimental results of the chemical composition analysis of the maximum saturation magnetization sample with the initial composition of Ca:La:Fe = 0.8:0.2:8.0 sintered at 1250°C. The compositions of Ca and La are similar to the initial amounts, but the composition of Fe is slightly larger than the initial amount. Therefore, the M-type ferrite was formed with the composition of  $\text{Ca}_{0.83}\text{La}_{0.17}\text{Fe}_{8.9}\text{O}_{19-\sigma}$ . The difference from the initial composition may be caused by low-melting-point calcium-iron oxides such as  $\text{CaFe}_2\text{O}_4$  that can be eluted off from the M-type grain.



**Fig. 5** X-ray diffraction patterns of  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_{8.0}\text{O}_{19-\sigma}$  ( $x = 0.1-0.3$ ) sintered at 1250°C.

**Table 1** Lattice constants of  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at 1250°C.

		$a(\text{\AA})$	$c(\text{\AA})$
$y = 0.8$ sintered at 1250°C	$x = 0.3$	5.892	22.98
	$x = 0.2$	5.887	23.00
	$x = 0.1$	5.894	23.03
SrFe <sub>12</sub> O <sub>19</sub> (SrM) <sup>14)</sup>		5.884	23.04
BaFe <sub>12</sub> O <sub>19</sub> (BaM) <sup>15)</sup>		5.889	23.22

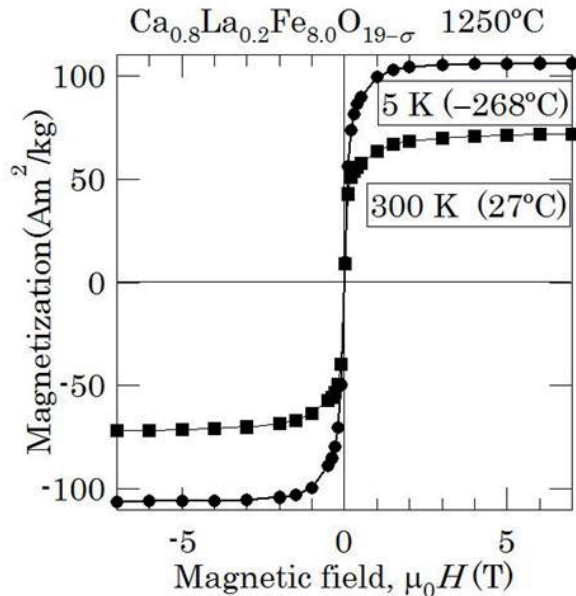


**Fig. 6** Temperature dependence of magnetization of  $\text{Ca}_{1-x}\text{La}_x\text{Fe}_{8.0}\text{O}_{19-\sigma}$  ( $x = 0.1-0.3$ ) sintered at 1250°C.

Figure 7 shows the magnetization curves at 5 K ( $-268^\circ\text{C}$ ) and 300 K ( $27^\circ\text{C}$ ) of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at 1250°C. The spontaneous magnetization at 5 K ( $-268^\circ\text{C}$ ) is estimated to be  $14.7 \mu\text{B}/\text{f.u}$  ( $104 \text{ Am}^2/\text{kg}$ ) by linear extrapolation of the magnetization curve from

**Table 2** The result of composition analysis of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at  $1250^\circ\text{C}$ .

Element	Average (at.%)
Ca	8.328
La	1.761
Fe	89.91
Fe/(Ca+La)	8.912



**Fig. 7** Magnetization curves at 5 K ( $-268^\circ\text{C}$ ) and 300 K ( $27^\circ\text{C}$ ) of  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{8.0}\text{O}_{19-\sigma}$  sintered at  $1250^\circ\text{C}$ .

the high field region of  $2 \leq \mu_0 H \leq 7$  T.

We would like to estimate the magnetic moment of the Ca-based hexaferrite. The hexaferrite ( $\text{MFe}_{12}\text{O}_{19}$ ;  $\text{M}=\text{Ba}^{2+}, \text{Sr}^{2+}$ ) consists of the R-block ( $[\text{MFe}_6\text{O}_{11}]^{2-}$ ) and the S-block ( $[\text{2Fe}_3\text{O}_4]^{2+}$ ), as shown in Fig. 1. The spin arrangements in the R- and S-blocks are similar to each other in spite of the different block structures. There is one central up-spin site between two down-spin sites in each block. There are three up-spin sites between the R-blocks and S-blocks. Therefore, the spin distribution is such that the number of up-spin sites is twice that of the down-spin sites (up:down = 2:1).

The EPMA analysis implied that the chemical formula was approximately  $\text{Ca}_{0.8}\text{La}_{0.2}\text{Fe}_{9.0}\text{O}_{14.6}$  as shown in Table 2. Here, the composition ratio of oxygen is estimated from the charge balance with the concentration of  $\text{Ca}^{2+}$ ,  $\text{La}^{3+}$ , and  $\text{Fe}^{3+}$  cations. In this chemical formula, six of nine spins are in up direction and the other three spins are in down direction with respect to the spin distribution ratio (up:down = 2:1). This estimated magnetic moment of  $15 \mu_B/\text{f.u.}$  is consistent with the observed magnetization at 5 K ( $-268^\circ\text{C}$ ).

#### 4. Conclusion

We have investigated the synthesis conditions and magnetic properties of Fe-deficient Ca-based M-type ferrite. The sintering temperature of the best sample was  $1250^\circ\text{C}$  and the analyzed composition was approximately  $\text{Ca}:\text{La}:\text{Fe} = 0.8:0.2:9.0$ . The saturation magnetization of the best sample was  $68.0 \text{ Am}^2/\text{kg}$  at room temperature and  $104 \text{ Am}^2/\text{kg}$  at 5 K ( $-268^\circ\text{C}$ ). The Curie temperature of this sample was about  $400^\circ\text{C}$ .

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# Study on Electromagnetic Levitation System for Ultrathin Flexible Steel Plate Using Magnetic Field from Horizontal Direction

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In the transport system of a thin-steel-plate production line, the quality of the plate surface deteriorates over time because of contact with rollers. As a solution to this problem, we have proposed the use of electromagnets to control the horizontal displacement of the steel plate. Vertical force to support the steel plate and horizontal force to suppress elastic vibration are applied to the steel plate by using the horizontal electromagnet. Focusing on these forces, we proposed a magnetic levitation system for the steel plate using only electromagnets installed in the horizontal direction. In this paper, the suspension force in the proposed system is analyzed by the finite element method, and the possibility of applying the proposed system for thinner steel plates is considered. Suspension force is effectively generated owing to the thinness of the steel plate. The results, indicate the proposed magnetic levitation system to be effective for thin steel plates. To verify the validity of the analytical conclusion, an electromagnetic suspension experiment has been carried out, and suspension force generated by the electromagnet has been measured. The agreement between the experimental and analytical results, confirmed the validity of the analytical results.

**Key words:** electromagnetic levitation, thin steel plate, noncontact support, finite element method

## 1. Introduction

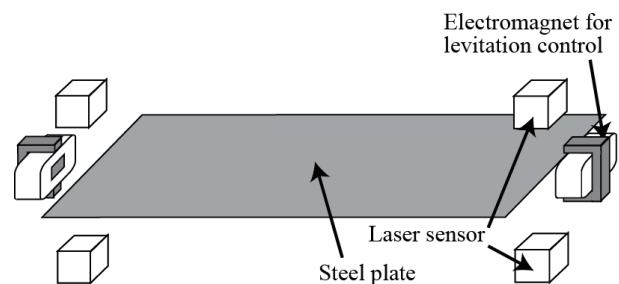
Thin steel plates are widely used in various industrial products. However, there are the problems of the deterioration of the surface quality and the occurrence of metal plating during transport owing to contact between the steel plate and rollers. As a solution to these problems, a noncontact transport of steel plates using electromagnetic force has been proposed<sup>1)-4)</sup>. However, in these considerations, electromagnets are installed in the vertical direction. In this method, if the steel plate is thin and does not have sufficient flexural rigidity, it is difficult to add suspension force for levitation over the entire steel plate. Previously, the electromagnetic levitation system for steel plates had electromagnets installed in the horizontal direction as well as the vertical direction. This system is able to transport a magnetically levitated steel plate<sup>5)</sup>. Moreover, a similar experiment for an ultrathin steel plate was performed, and the noncontact transport of ultrathin steel plates was demonstrated<sup>6)-7)</sup>. However, since this proposed system requires a number of control channels, there are the problems of complexity and high cost.

Because of the magnetic field of the added electromagnets, attractive force acts in the steel plate as the vertical suspension force as well as the horizontal tension force. The tension force can add the suspension force to the entire steel plate, and it becomes possible to improve the levitation stability. Moreover, the tension can prevent the plastic deformation of the steel plate, such as dimpling and folding. This can be expected to lead to surface quality improvement of the steel plate. Focusing on these forces, the feasibility of a magnetic levitation system for steel plates using only electromagnets installed in the horizontal direction was

considered. Electromagnetic field analysis by the finite element method (FEM) was performed, and we confirmed that the proposed system could levitate a steel plate with a thickness of 0.3 mm<sup>8)</sup>. However, these results have not been verified experimentally. Furthermore, the effectiveness of this system for thinner steel plates has not been considered. In this study, the suspension force in the proposed system is analyzed by the FEM and the applicability of the proposed system to thinner steel plates is considered. In addition, electromagnetic suspension experiments are performed with the steel plate thickness of 0.30 mm or 0.24 mm. To show the effectiveness of this system for thinner steel plates, analytical and experimental results are discussed in detail.

## 2. FEM analyses of suspension force of electromagnet

Figure 1 shows an outline of the proposed system. A zinc-coated steel plate is levitated and positioned in the noncontact mode by the attractive forces of electromagnets that are controlled on the basis of feedback signals from laser sensors.



**Fig. 1** Electromagnetic levitation system for steel plate using only electromagnets installed in horizontal direction.



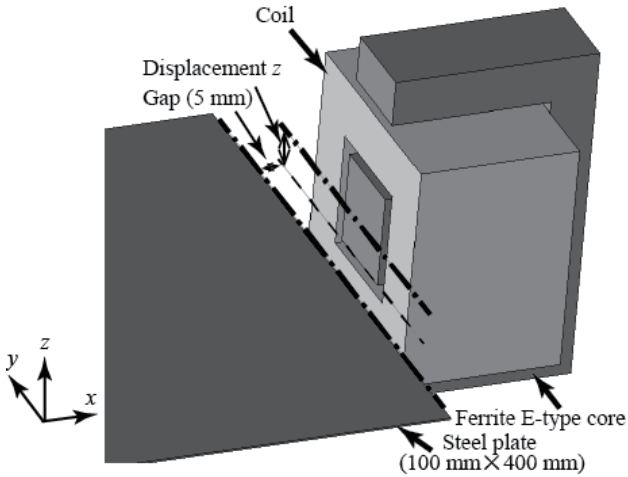


Fig. 2 FE analytical model.

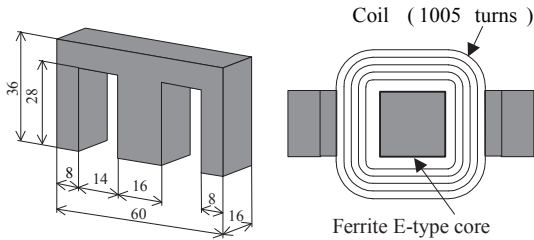


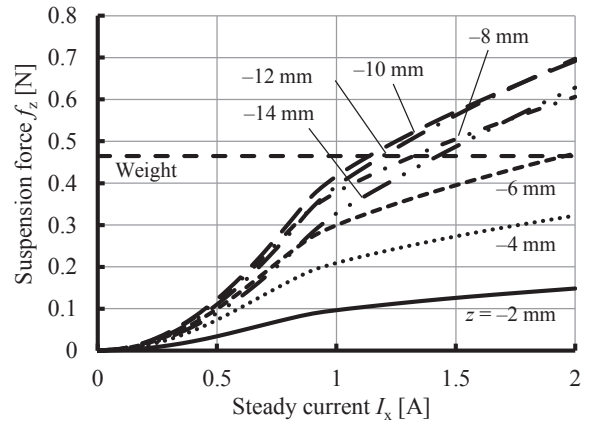
Fig. 3 Schematic illustration of electromagnet.

In the previous study<sup>7)</sup>, it has been confirmed that this control system can control horizontal displacement of the steel plate (length 400 mm, width 100 mm, thickness 0.18 mm, material SS400 steel), and suppress the standard deviation of horizontal displacement less than 0.1 mm. From the above, it was confirmed that the proposed system has a practically sufficient control performance for positioning control in the horizontal direction.

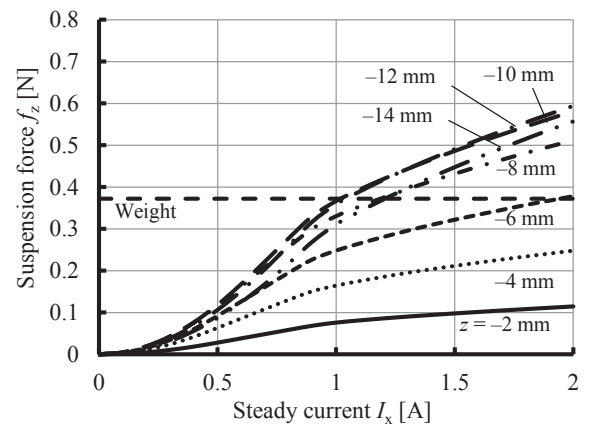
2.1 FE model and analytical conditions

To discuss the effectiveness of this system, suspension force is analyzed by the FEM. The electromagnetic field analysis is carried out using the finite-element method software JMAG (Ver. 11). The analytical model is shown in Fig. 2. The steel plate (length 400 mm, width 100 mm, material SS400 steel) is levitated with electromagnets shown in Fig. 3. In previous studies<sup>8)</sup>, analytical results showed that this electromagnet can generate a sufficient horizontal tension for positioning control more than 2 times greater than vertical suspension force. Furthermore, it has been confirmed that the steel plate is hardly displaced in the control direction with horizontal positioning control<sup>7)</sup>. Therefore, the analysis is carried out on the assumption that the steel plate does not displace from the control point.

The analytical conditions are as follows. Vertical displacement  $z$  is changed from  $-2$  mm to  $-14$  mm. The gap between the edge of the steel plate and the surface of electromagnets is 5 mm. The steady electromagnet current  $I_x$  is in the range from 0.1 A to 2.0 A. The



(a) Thickness  $h = 0.30$  mm



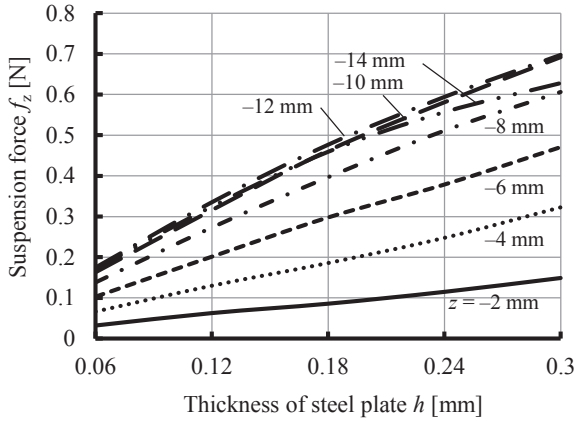
(b) Thickness  $h = 0.24$  mm

Fig. 4 Relationship between thickness of steel plate  $h$  and vertical attractive force  $f_z$  for each displacement  $z$ .

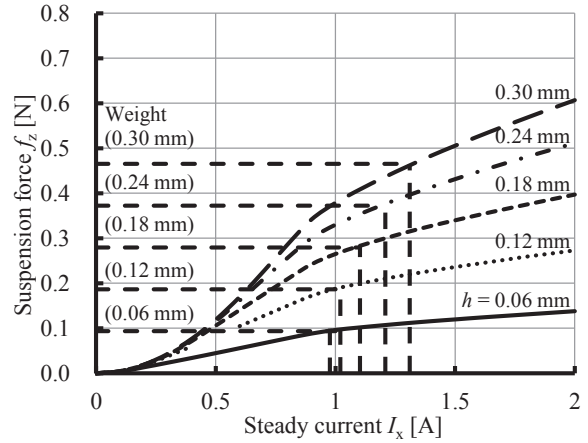
thickness of the steel plate  $h$  is changed from 0.06 mm to 0.30 mm with each increase in thickness of 0.06 mm.

2.2 Numerical results by FEM

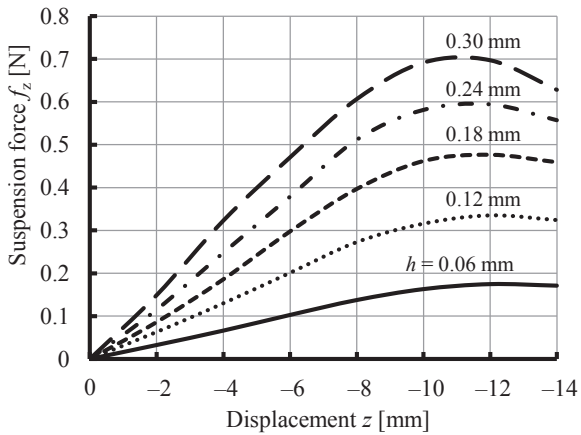
Figure 4 shows the relationship between steady current  $I_x$  [A] and vertical suspension force  $f_z$  [N]. Figure 4(a) shows the analytical result for the steel plate with a thickness of 0.30 mm. Figure 4(b) shows the result for a plate thickness of 0.24 mm. Dotted lines in these figures mean the weight of the steel plate. If the generated suspension force is equal to the weight of the steel plate, the steel plate can be levitated. Analytical results show that increasing the steady current leads to upward displacement of the steel plate. When the steady current is greater than 1.0 A, the suspension force is increased gradually, because magnetic saturation occurs in the core. When the steel plate is displaced downward, suspension force increases. The results in Fig 4(a) indicate that the steel plate can be levitated when displacement is greater than  $-6$  mm. However, even if the steel plate is displaced more than  $-10$  mm, suspension force does not increase further. The cause of this result is the magnetic field generated from the convex portion of the lower part of the electromagnet core. Although suspension force



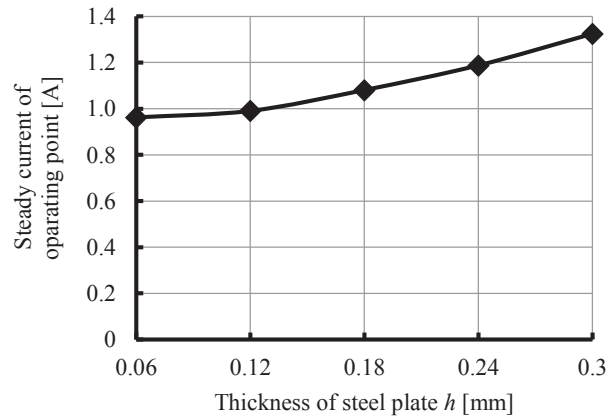
**Fig. 5** Relationship between thickness of steel plate  $h$  and suspension force  $f_z$  for each displacement  $z$  (steady current  $I_x = 2.0$  A).



**Fig. 7** Relationship between steady current  $I_x$  and suspension force  $f_z$  for each thickness of steel plate  $h$  (displacement  $z = -8$  mm).



**Fig. 6** Relationship between displacement  $z$  and suspension force  $f_z$  for each thickness of steel plate  $h$  (steady current  $I_x = 2.0$  A).



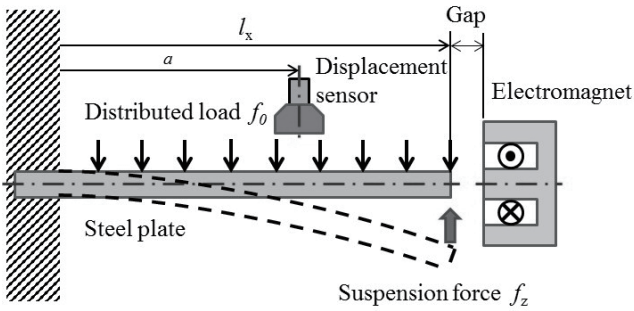
**Fig. 8** Relationship between thickness of steel plate  $h$  and steady current of operating point (displacement  $z = -8$  mm).

generally decreases, the result for the plate with 0.24 mm thickness shows the same tendency as that for the plate with 0.30 mm thickness, as shown in Fig. 4(b).

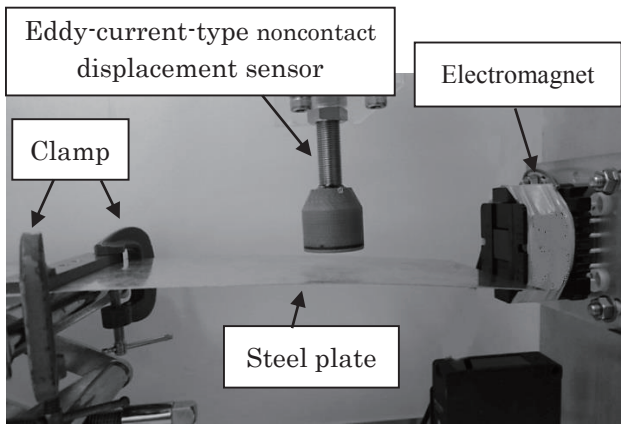
Figure 5 shows the relationship between plate thickness and suspension force for each displacement when the steady current is 2.0 A at maximum. The suspension force is reduced in proportion to the decrease in the thickness. The reason for this is considered that the part for generating suspension force becomes smaller when the thickness of steel plate is thinner. Figure 6 shows the relationship between suspension force and displacement for each thickness when the steady current is 2.0 A. The suspension force is linearly proportional to the displacement when the displacement is less than -8 mm. In this linear range, even if the steel plate is vertically displaced by a disturbance, the suspension force acts as a restoring force. With this restoring force, the steel plate stabilizes passively.

Figure 7 shows the relationship between steady current and suspension force for each thickness of steel

plate with  $z = -8$  mm. The dotted lines indicate the weight of the steel plate for each thickness. At the operating point where suspension force is equal to its own weight, the steel plate can be levitated. As the steel plate becomes lighter when it becomes thinner, it seems to be more easily levitated. On the other hand, the suspension force is also decreased. From these analytical result, it is found that the decrease in the suspension force is smaller than the decrease in the weight of the steel plate. These results show that decreasing the thickness of the steel plate can reduce the steady current of the operating point. The relationship between the thickness of the steel plate and the steady current of the operating point is shown in Fig. 8. Compared with the result for the thickness of 0.30 mm, the steady current of the operating point is reduced 18.4% in the case of the 0.18 mm thickness, and 27.3% in the case of the 0.06 mm thickness. Suspension force is more effectively generated with increasing thinness of the steel plate. The proposed magnetic levitation system is superior for thin steel plates that are difficult to levitate by the conventional method.



**Fig. 9** Experimental model of electromagnetic suspension force.



**Fig. 10** Photograph of experimental apparatus for electromagnetic suspension.

### 3. Electromagnetic suspension experiment

#### 3.1 Experimental model

To verify the validity of the above analytical results, the electromagnetic suspension experiment is carried out. Experimental model is shown in Fig. 9. An electromagnet is installed near the end of the fixed steel plate. An eddy-current-type noncontact displacement sensor is installed above the steel plate to measure the displacement of the steel plate. Distributed and concentrated loads act on the steel plate. Distributed load is due to its own weight, and concentrated load is due to suspension force by from the electromagnet.

Vertical displacement  $z'$  [m] of the steel plate without suspension force  $f_z$  [N] from the electromagnet and vertical displacement  $z$  [m] with  $f_z$  are expressed as <sup>9)</sup>

$$z'(x) = \frac{f_0}{EI} \left( \frac{1}{24}x^4 - \frac{l_x}{6}x^3 + \frac{l_x^2}{4}x^2 \right) \quad (1)$$

$$z(x) = z'(x) + \frac{f_z}{EI} \left( -\frac{1}{6}x^3 + \frac{l_x}{2}x^2 \right). \quad (2)$$

Distributed load  $f_0$  [N/m] due to self-weight is expressed as

$$f_0 = \rho g h l_y, \quad (3)$$

where  $x$  is the horizontal displacement [m],  $l_x$  the length of the steel plate [m],  $l_y$  the width of the steel plate [m],  $h$

**Table 1** Parameters and values.

Parameter	Value
$\rho$	7500 kg/m <sup>3</sup>
$l_x$	0.20 m
$l_y$	0.10 m
$h$	0.30×10 <sup>-3</sup> m, 0.24×10 <sup>-3</sup> m
$a$	0.115 m
$E$	206 GPa
$g$	9.81 m/s <sup>2</sup>

the thickness of steel plate [m],  $\rho$  the plate density [kg/m<sup>3</sup>],  $g$  the acceleration due to gravity [m/s<sup>2</sup>],  $E$  Young's modulus of the thin steel plate [N/m<sup>2</sup>],  $I$  the second moment of area [m<sup>4</sup>], and  $a$  the sensor position from the fixed end [m].

Suspension force  $f_z$  is obtained by measuring displacements  $z$  and  $z'$  at sensor position  $a$ , as

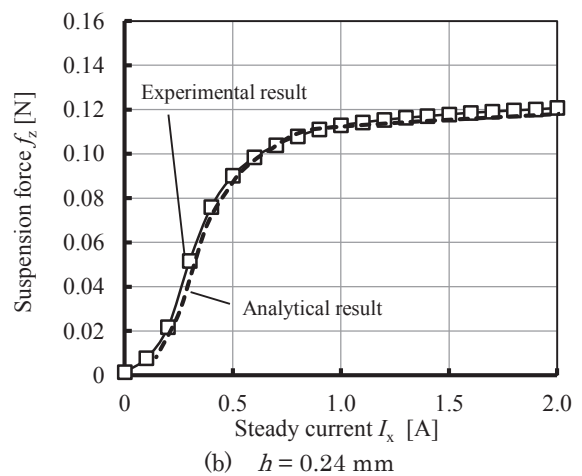
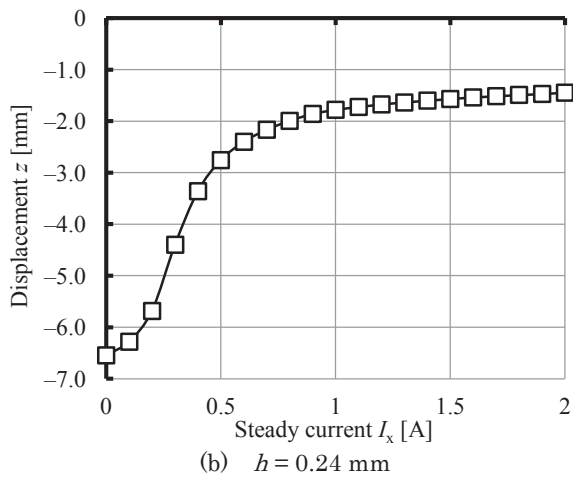
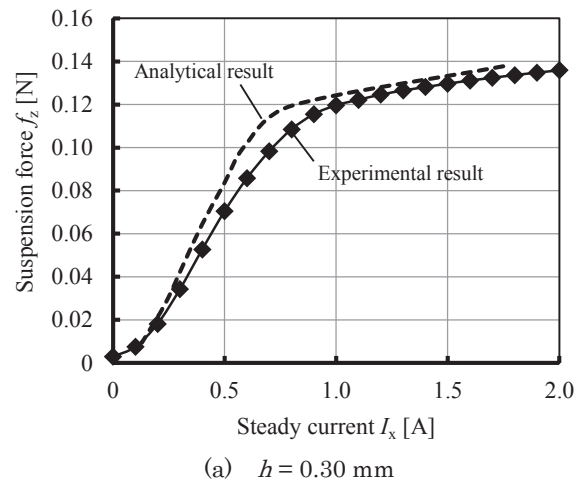
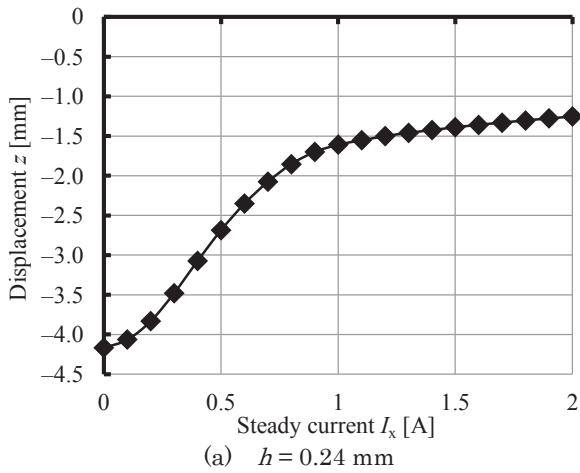
$$f_z = \frac{EI}{-\frac{1}{6}a^3 + \frac{l_x}{2}a^2} (z(a) - z'(a)) \quad (4)$$

#### 3.2 Experimental conditions

Table 1 shows the specifications of the experiment. Figure 10 is the photograph of the experimental apparatus for electromagnetic suspension. The steel plate is fixed with clamps. In the vertical direction, the electromagnet is installed at the same position as the supporting position. The gap between the surface of the electromagnet and the edge of the steel plate end is 5 mm. Vertical displacement of the steel plate is measured with a sensor when the steady current of the electromagnet is changed from 0 A to 2.0 A. In this experiment, the edge of the steel plate tilts about 5° due to deflection. This experimental condition is different from analytical condition in chapter 2. However, the attractive force generates locally at the only edge of steel plate<sup>8)</sup>. Furthermore, we analyzed previously the attractive force generated at steel plate when the steel plate tilts 5°. Comparing analytical result of tilt angle 0° and 5°, amount of change of the suspension force  $f_z$  was less than 5%. Therefore, it is confirmed that the deflection of the steel plate does not affect suspension force.

#### 3.3 Experimental results

Figure 11 shows the relationship between steady current and displacement. Figure 11 (a) shows the result for the plate with 0.30 mm thickness. Figure 11 (b) shows the result for the plate with 0.24 mm thickness. Previously, the experimental value measured with a sensor was compared with the calculated value with the steady current of 0 A. The result has confirmed that the differences between experimental and calculated values



**Fig. 11** Relationship between steady current  $I_x$  and measured displacement  $z$  by sensor.

**Fig. 12** Relationship between steady current  $I_x$  and calculated suspension force  $f_z$  for measured displacement and analytical results

are less than 1%. Experimental results show that increasing the steady current leads to upward displacement of the steel plate. This trend is significant when the steady current is less than 0.5 A.

Figure 12 shows the relationship between steady current and suspension force calculated using the experimental result. Figure 12 (a) shows the result for the plate with 0.30 mm thickness. Figure 12 (b) shows the result for the plate with 0.24 mm thickness. The plotted point in this figures indicate experimental results. Suspension force increases with increasing steady current. When the steady current is less than 0.5 A, the increment of suspension force is larger. The attractive force of the electromagnet is generated at the steel plate toward the center of the electromagnet core. If the steel plate is displaced further downward, the ratio of suspension force to attractive force is larger. On the other hand, when the steel plate is displaced upward, the ratio of tension to attractive force is larger. It is considered that the cause of saturation is upward displacement of the steel plate.

Dashed line in Fig. 12 indicates analytical results of suspension force. This analytical suspension force is calculated using eq. (2) when the displacement of the

edge of steel plate coincides analysis condition in chapter 2. The analytical steady current is obtained using Fig. 4 when the displacement and analytical suspension force coincides analysis condition.

The experimental results agree the analytical results. In the range of size in this paper, deflection of the steel plate was experimentally confirmed that seldom effect on the suspension force. Furthermore, the agreement of the analytical and experimental results shows the validity of the realization of the magnetic levitation system only using electromagnets in the horizontal direction described in the previous section.

#### 4. Conclusion

In our proposed system using only electromagnets installed in the horizontal direction, vertical suspension force, which was applied to the steel plate by an electromagnet, was analyzed for a steel plate thickness of less than 0.30 mm. In the range of interest in this study, suspension force is more effectively generated as the steel plate becomes thinner. The results indicate the proposed magnetic levitation system to be superior for thin steel plates. To verify the validity of the analytical conclusion,



an electromagnetic suspension experiment was carried out using an experimental apparatus for electromagnetic suspension, and suspension force of the electromagnet was measured. The agreement between the experimental and analytical results showed the validity of the analysis.

In the next stage, in order to realize a magnetic levitation system for noncontact transport and suspension of steel plates, a system with improved stability will be designed by installing more electromagnets.

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